

# The Myth of Long-Horizon Predictability

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The prevailing view in finance is that the evidence for long-horizon stock return predictability is significantly stronger than that for short horizons. We show that for persistent regressors, a characteristic of most of the predictive variables used in the literature, the estimators are almost perfectly correlated across horizons under the null hypothesis of no predictability. For the persistence levels of dividend yields, the analytical correlation is 99% between the 1- and 2-year horizon estimators and 94% between the 1- and 5-year horizons. Common sampling error across equations leads to ordinary least squares coefficient estimates and  $R^2$ s that are roughly proportional to the horizon under the null hypothesis. This is the precise pattern found in the data. We perform joint tests across horizons for a variety of explanatory variables and provide an alternative view of the existing evidence. (*JEL* G12, G14, C12)

Over the last two decades, the finance literature has produced growing evidence of stock return predictability, though not without substantial debate. The strongest evidence cited so far comes from long-horizon stock returns regressed on variables such as dividend yields, term structure slopes, and credit spreads, among others. A typical view is expressed in Campbell, Lo, and MacKinlay's (1997, p.268) standard textbook for empirical financial economics, *The Econometrics of Financial Markets*:

At a horizon of 1-month, the regression results are rather unimpressive: The  $R^2$  statistics never exceed 2%, and the  $t$ -statistics exceed 2 only in the post-World War II subsample. The striking fact about the table is how much stronger the results become when one increases the horizon. At a 2-year horizon the  $R^2$  statistic is 14% for the full sample . . . at a 4-year horizon the  $R^2$  statistic is 26% for the full sample.

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However, there is an alternative interpretation of this evidence: researchers should be equally impressed by the short- and long-horizon evidence for the simple reason that the regressions are almost perfectly correlated. For an autocorrelation of 0.953 for annual dividend yields, we show analytically that the 1-year and 2-year predictive estimators are 98.8% correlated under the null hypothesis of no predictability. For longer horizons, the correlations are even higher, reaching 99.6% between the 4- and 5-year horizon estimators. This degree of correlation manifests itself in multiple-horizon regressions in a particularly unfortunate way. Since the sampling error that is almost surely present in small samples shows up in each regression, both the estimated coefficient and  $R^2$  are proportional to the horizon.

This article provides analytical expressions for the correlations across multiple-horizon estimators, and then shows through simulations that these expressions are relevant in small samples. The analytical expressions relate the correlations across these estimators to both the degree of overlap across the horizons and the level of persistence of the predictive variable. Our findings relate to an earlier literature looking at joint tests of the random walk hypothesis for stock prices using multiple-horizon variance ratios and autocorrelations, among other estimators [e.g., Richardson and Smith (1991, 1994) and Richardson (1993)]. This earlier work stresses accounting for the degree of overlap. The problem here is much more severe. In the univariate framework, the predictive variable—past stock returns—is approximately independently and identically distributed (IID). In this article's framework, the predictive variable, for example dividend yields, is highly persistent.

Our simulations show that any sampling error in the data, under the null hypothesis of no predictability, appears in the same manner in every multiple-horizon regression when the predictive variable is highly persistent. Using box plots and tables describing the relation across the multiple-horizon estimates and  $R^2$ s, we show the exact pattern one should expect under the null hypothesis: the multiple-horizon estimates are monotonic in the horizon approximately two-thirds of the time, and the mean ratios of the 2- to 5-year estimators to the 1-year estimator are 1.93, 2.80, 3.59, and 4.32, respectively. Consider the actual estimated coefficients for the regression of 1- to 5-year stock returns on dividend yields over the 1926–2004 sample period: 0.131, 0.257, 0.390, 0.461, and 0.521. These correspond to monotonically increasing estimates with corresponding ratios of 1.96, 2.98, 3.53, and 3.99. We show that these estimates lie in the middle of the distribution of possible outcomes under the null hypothesis.

The theoretical and simulation analyses stress the importance of interpreting the evidence jointly across horizons. We develop an analytical expression for a joint test based on the Wald statistic. While a high level

of persistence means that it can be dangerous to interpret regressions over multiple horizons, the joint tests show that this persistence may lead to powerful tests for economies in which predictability exists. Such predictability may take a particular form, in which the multiple-horizon coefficients are much less tied together than the null hypothesis implies. Applying the joint tests to commonly used predictive variables, we point out various anomalies and contrast our results with the conclusions of the existing literature.

Among the standard set of variables, none generate joint test statistics that are significant at the 10% level under the simulated distribution. Interestingly, the only variable that is significant at the 10% level under the asymptotic distribution is the risk-free rate, despite the fact that the associated horizon-by-horizon  $p$ -values are larger and the  $R^2$ s are smaller than for many of the other variables, including the dividend yield and the book-to-market ratio. Among more recently developed variables, joint tests confirm the ability of both the net payout yield [Boudoukh, Michaely, Richardson, and Roberts (2005)] and the equity share of new issuances [Baker and Wurgler (2000)] to forecast stock returns across all horizons.

The article proceeds as follows. In Section 1, we provide the expressions for analyzing multiple-horizon regressions and show that the basic findings carry through to small samples. Section 2 applies the results to a number of data series and evaluates existing evidence using joint tests of predictability. Section 3 concludes.

## **1. Multiple-Horizon Regressions**

### **1.1 The existing literature**

Fama and French (1988a) is the first article to document evidence of multivariate stock return predictability over multiple horizons.<sup>1</sup> In brief, they regress overlapping stock returns of 1 month to 4 years on dividend yields, reporting coefficients and  $R^2$ s that increase somewhat proportionately with the horizon. As it documents what has become one of the dominant stylized facts in empirical finance, this article has over 250 citations to date. To illustrate one common view, consider part of John Cochrane's (1999, p.37) description of the three most important facts in finance in his survey, *New Facts in Finance*.

Now, we know that . . .

[Fact] 2. Returns are predictable. In particular: Variables including the dividend/price (d/p) ratio and term premium can predict substantial amounts of stock return variation. This phenomenon occurs over

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<sup>1</sup> See also Campbell and Shiller (1988).

business cycle and longer horizons. Daily, weekly, and monthly stock returns are still close to unpredictable. . .

This fact is emphasized repeatedly in other surveys (e.g., Fama (1998, p.1578), Campbell (2000, p.1522 and 2003, p.5) and Barberis and Thaler (2003, p.21), among others), is often used to calibrate theoretical models (among others, Campbell and Cochrane (1999a, p.206), Campbell and Viceira (1999b, p.434), Barberis (2000, p.225), Menzly, Santos, and Veronesi (2004, p.2), and Lettau and Ludvigson (2005, p.584)), and motivates new empirical tests (e.g., Ferson and Korajczyk (1995, p.309), Patelis (1997, p.1951), Lettau and Ludvigson (2001, p.815), and Ait-Sahalia and Brandt (2001, p.1297)).

However, this interpretation of the evidence does not have universal support. Three principal alternative lines of criticism have been put forward in the literature. The first involves data snooping, which is perhaps best described by Foster, Smith, and Whaley (1997). The idea is that the levels of predictability found at short horizons are not surprising, given the number of variables from which researchers can choose. Various articles provide some support for these findings, including Bossaerts and Hillion (1999), Cremers (2002), and Goyal and Welch (2005).

A second approach looks at the small sample biases of the estimators. Stambaugh (1999) shows that the bias can be quite severe, given the negative correlation between contemporaneous shocks to returns and the predictive variable, which usually involves some type of stock price deflator.<sup>2</sup> His findings suggest much less predictability once the estimators are adjusted for this bias. However, Lewellen (2004) argues that the effect of the bias may be much smaller if one takes the persistence of the predictive variable into account. Lewellen's approach is similar to Stambaugh's (1999) Bayesian analysis of the predictability problem. While these articles certainly question the magnitude of the predictability, they do not address long-horizon predictability *per se*.

The third line of criticism, first explored by Richardson and Stock (1989) in a univariate setting, uses an alternative asymptotic theory, in which the horizon increases with the sample size. Valkanov (2003) argues that long-horizon regressions have poor properties relative to standard asymptotics.<sup>3</sup> He shows that the estimators may no longer be consistent and have limiting distributions that are functionals of Brownian motions; in fact, the distributions are not normal and are not centered on the true

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<sup>2</sup> Other articles that look at other small sample issues such as persistence and spurious regression, as well as this bias, include Foster, Sarkissian and Simin (2003), Jansson and Moreira (2006), Amihud and Hurvich (2004), Torous, Valkanov and Yan (2004), Campbell and Yogo (2006), and Powell, Shi, Smith and Whaley (2005).

<sup>3</sup> Ang and Bekaert (2005) show that the statistical significance of long horizon regressions is overstated once the researcher adjusts for heteroskedasticity and the overlapping errors by imposing the null in estimation.

coefficient. Valkanov then shows that this alternative asymptotic theory works better in small samples. His results can be viewed as the theoretical foundation for earlier simulated distributions by Kim and Nelson (1993) and Goetzmann and Jorion (1993), and for the intuition put forward by Kirby (1997), who uses standard asymptotics.

Nevertheless, even in the face of these criticisms, the evidence for predictability is commonly cited. One reason may be that the literature has been able to tie the different magnitudes of predictability at short and long horizons together in a consistent way. For example, it is fairly well known since Fama and French (1988), and in particular from Campbell (2001), that the key determinants of long-horizon predictability are the extent of predictability at short horizons and the persistence of the regressor. The  $R^2$ s at long horizons relative to a single-period  $R^2$  are a function of the latter (see also the previously cited texts, Cochrane (2001, p. 393) and Campbell, Lo and MacKinlay (1997, p. 271)). Holding everything else constant—single-period predictability in particular—higher persistence results in a higher fraction of explainable long-horizon returns. As a function of the horizon, the  $R^2$  first rises with the horizon, but eventually decays, because of the exponential decline in the informativeness of the predictive variable. As we show below, persistence also matters in the case of no predictability, but in the presence of sampling error.

Our article focuses on the joint properties of the regression estimators across horizons, and our conclusions closely resemble those of Richardson and Smith (1991) and Richardson (1993) regarding long-horizon evidence against the random walk in Fama and French (1988b) and Poterba and Summers (1988). In many ways the arguments here are more damaging because we show that the degree of correlation across the multiple-horizon estimators is much higher than it is in the case of long-horizon tests for the random walk. In fact, the null hypothesis of no predictability implies the exact pattern in coefficients and  $R^2$ s found in articles presenting evidence in favor of predictability. We show these results in the next two subsections.

## 1.2 Statistical properties

We consider regression systems of the following type:

$$\begin{aligned}
 R_{t,t+1} &= \alpha_1 + \beta_1 X_t + \varepsilon_{t,t+1} \\
 &\vdots \\
 R_{t,t+j} &= \alpha_j + \beta_j X_t + \varepsilon_{t,t+j}, \\
 &\vdots \\
 R_{t,t+J} &= \alpha_J + \beta_J X_t + \varepsilon_{t,t+J}
 \end{aligned} \tag{1}$$

where  $R_{t,t+j}$  is the  $j$ -period stock return,  $X_t$  is the predictor, for example the dividend yield, and  $\varepsilon_{t,t+j}$  is the error term over  $j$  periods. As is well-known from Hansen and Hodrick (1980) and Hansen (1982), among others, the error terms are serially correlated because of overlapping observations. Using the standard generalized method of moments calculations under the null hypothesis of no predictability and conditional homoskedasticity (e.g., Richardson and Smith (1991)), in the Appendix we derive the covariance matrix of  $\hat{\beta}_j$  and  $\hat{\beta}_k$  for any two horizons,  $j$  and  $k$ :

$$T\text{Var}(\hat{\beta}_j, \hat{\beta}_k) = \frac{\sigma_R^2}{\sigma_X^2} \begin{pmatrix} j + 2 \sum_{l=1}^{j-1} (j-l)\rho_l & j + \left[ \sum_{l=1}^{j-1} (j-l)(\rho_l + \rho_{l+(k-j)}) \right. \\ & \left. + \sum_{l=1}^{k-j} j\rho_l \right] \\ \dots & k + 2 \sum_{l=1}^{k-1} (k-l)\rho_l \end{pmatrix}, \quad (2)$$

where  $k > j$ ,  $\rho_l$  is the  $l^{\text{th}}$ -order autocorrelation of  $X_t$ , and  $\sigma_R^2$  and  $\sigma_X^2$  are the variances of the one-period return and the predictor, respectively. The above expression for the covariance matrix of the estimators is not particularly intuitive, though it is immediately apparent that for  $j$  close to  $k$  the estimators are almost perfectly correlated. Less obvious is the fact that for  $\text{cov}(X_t, X_{t-l}) \approx \sigma_X^2$  the estimators are also almost perfectly correlated irrespective of the horizon. Intuitively, the persistence of  $X_t$  acts in much the same way as overlapping horizons in terms of the limited amount of independent information across multiple horizons.

A popular simplification is to assume that  $X_t$  follows an AR(1) [see, among others, Campbell (2001), Boudoukh and Richardson (1994), Stambaugh (1993), and Cochrane (2001)]. Under the AR(1) model,  $\text{cov}(X_t, X_{t-l}) = \rho^l \sigma_X^2 = \rho^l \sigma_X^2$  where  $\rho$  is the autoregressive parameter for  $X_t$ , and the covariance matrix in Equation (2) reduces to a much simpler form:

$$T\text{Var}(\hat{\beta}_j, \hat{\beta}_k) = \frac{\sigma_R^2}{\sigma_X^2} \begin{pmatrix} j + \frac{2\rho}{(1-\rho)^2} [(j-1) - \rho(j-\rho^{j-1})] & j + \frac{\rho}{(1-\rho)^2} \{ 2[(j-1) - \rho(j-\rho^{j-1})] \\ & + (1-\rho^j)(1-\rho^{k-j}) \} \\ \dots & k + \frac{2\rho}{(1-\rho)^2} [(k-1) - \rho(k-\rho^{k-1})] \end{pmatrix}. \quad (3)$$

For the special case of  $j = 1$ , the correlation with horizon  $k$  is

$$\frac{(1-\rho)^2 + \rho(1-\rho)(1-\rho^{k-1})}{\sqrt{(1-\rho)^2} \sqrt{k(1-\rho)^2 + 2\rho[(k-1) - \rho(k-\rho^{k-1})]}}. \quad (4)$$

For example, for  $k = 2$ , we get  $\sqrt{\frac{1+\rho}{2}}$ . In our sample, the autocorrelation of the dividend yield is 0.953, which yields a correlation of 0.988 between the 1- and 2-year estimators. As the horizon  $k$  increases to 3, 4, and 5 years, the correlations fall only slightly to 0.974, 0.959, and 0.945, respectively.<sup>4</sup> Even at a 10-year horizon, the correlation is over 87%. With the typical sample sizes faced by researchers in the field of empirical finance, these results suggest that one has to be extremely cautious in interpreting the coefficients separately.

For the typical 1- through 5-year horizons examined in the literature, the analytical covariance matrix of the estimators under the null hypothesis of no predictability and the dividend yield's  $\rho$  of 0.953 is

$$T\text{Var}(\hat{\beta}_{1-5}) = \frac{\sigma_R^2}{\sigma_X^2} \begin{pmatrix} 1 & 0.988 & 0.974 & 0.959 & 0.945 \\ & 1 & 0.993 & 0.982 & 0.970 \\ & & 1 & 0.995 & 0.986 \\ & & & 1 & 0.996 \\ & & & & 1 \end{pmatrix}. \quad (5)$$

Several observations are in order. First, the high degree of correlation across the multi-period estimators implies that under the null hypothesis, the regressions are essentially redundant. Second, under the null hypothesis, the estimators are asymptotically distributed as multivariate normal with a mean of zero. While this is clearly not true in small samples,<sup>5</sup> consider using this distribution to understand the effect of sampling error across the equations. Specifically, conditional on  $\hat{\beta}_1$  equal to  $\bar{\beta}_1$ , what do we expect  $\hat{\beta}_k$  to be under the null? Using the properties of a bivariate normal, we can write<sup>6</sup>

$$E[\hat{\beta}_k | \hat{\beta}_1 = \bar{\beta}_1] = \left(1 + \frac{\rho(1 - \rho^{k-1})}{1 - \rho}\right) \bar{\beta}_1. \quad (6)$$

For  $\rho$  close to 1, the coefficients should basically be proportional to the horizon. As an example, for  $\rho = 0.953$  the expected values of  $\hat{\beta}_k$ , in terms of  $\bar{\beta}_1$ , are  $1.953\bar{\beta}_1$ ,  $2.861\bar{\beta}_1$ ,  $3.727\bar{\beta}_1$ , and  $4.552\bar{\beta}_1$  for the 2-, 3-, 4-, and 5-year horizon regressions, respectively. Similarly, for the  $R^2$  of the

<sup>4</sup> Of course, these correlations are even larger as  $j$  increases for a fixed  $k$ .

<sup>5</sup> See Stambaugh (1999) for small sample bias and Valkanov (2003) for non-normality of the distributions of the estimators.

<sup>6</sup> Note that Cochrane (2001, p. 392) reports related results for the 1-year and 2-year slopes of the regression system in equation (1) under the alternative of predictability. These similarities serve to illustrate the difficulty in differentiating between the null of no predictability and the alternative.

regression,

$$E \left[ R_k^2 | R_1^2 = \bar{R}_1^2 \right] = \frac{\left( 1 + \frac{\rho(1-\rho^{k-1})}{1-\rho} \right)^2}{k} \bar{R}_1^2. \quad (7)$$

For  $\rho$  close to 1, the  $R^2$ s also increase significantly with the horizon. Again for  $\rho = 0.953$ , the ratios of the  $R^2$ s are 1.907, 2.729, 3.472, and 4.143 for the 2-, 3-, 4-, and 5-year horizon regressions, respectively.

The intuition is straightforward. Compare the regression of  $R_{t,t+1}$  on  $X_t$  to that of  $R_{t,t+k}$  on  $X_t$ . The former regression involves summing the cross products of the sequence of  $R_{t,t+1}$  and  $X_t$  for all  $t$  observations. Note that for a persistent series  $X_t$ , there is very little information across the sequence of  $X_t$  values. Thus, when an unusual draw from  $R_{t,t+1}$  occurs (denote it  $R_{t^*,t^*+1}$ ), and this observation happens to coincide with the most recent value of the predictive variable,  $X_{t^*}$ , it will also coincide with all the surrounding  $X_t$  observations, such as  $X_{t^*-1}$ ,  $X_{t^*-2}$ , and  $X_{t^*-3}$ . Since  $R_{t^*,t^*+1}$  shows up in  $k$  of the long-horizon returns  $R_{t,t+k}$  within the sample period (i.e., in  $R_{t^*+1-k,t^*+1}$ ,  $R_{t^*+2-k,t^*+2}$ , . . . ,  $R_{t^*,t^*+k}$ ), the impact of the unusual draw will be roughly  $k$  times larger in the long-horizon regression than in the one-period regression.

### 1.3 Joint tests

At first glance, the results in Section 1.2 provide a fairly devastating critique of the strategy of running multiple long-horizon regressions. However, this view is not necessarily accurate. Because the regressions are linked so closely under the null hypothesis, joint tests may have considerable power under alternative models.

What are these alternatives? The models must be such that the long horizons pick up information not contained in short horizons. The standard model, in which short-horizon returns are linear in the current predictor and that predictor follows a persistent autoregressive moving average (ARMA) process, is clearly not a good candidate. It would be optimal to focus on estimating the short-horizon and the ARMA process directly in this case (e.g., Campbell (2001), Hodrick (1992), and Boudoukh and Richardson (1994), among others). It should be noted though, that the standard model is often chosen for reasons of parsimony rather than on an underlying theoretical basis.

Consider testing the null of no predictability in the regression system given in equation (1), i.e.,  $\beta_1 = \dots = \beta_j = \dots = \beta_J = 0$ . The corresponding Wald Test statistic for this hypothesis is  $T \hat{\beta}' V(\hat{\beta})^{-1} \hat{\beta}$  where  $\hat{\beta}' = (\hat{\beta}_1 \dots \hat{\beta}_j \dots \hat{\beta}_J)$  and  $V(\hat{\beta})$  is the covariance matrix of the  $\hat{\beta}$  estimators

with typical elements given by  $\text{Var}(\hat{\beta}_j, \hat{\beta}_k)$  as shown in Equation (2).<sup>7</sup> The statistic follows an asymptotic chi-squared distribution with degrees of freedom given by the number of horizons used in estimation. Note that  $V(\hat{\beta})$  is a function of the autocorrelation structure of the  $X_t$  variable (i.e., its persistence) as well as the degree of overlap between horizons, i.e.,  $j$  versus  $k$ . Aside from the magnitude of the  $\hat{\beta}$  estimators, what matters is whether the pattern in  $\hat{\beta}$  across horizons is consistent with the correlation implied by  $V(\hat{\beta})$ .

To see this, consider performing a Wald Test of the hypothesis  $\beta_1 = \beta_2 = 0$ . The corresponding Wald statistic is given by

$$T \frac{\sigma_X^2}{\sigma_R^2} \left[ \frac{\frac{2\beta_1^2 + \beta_2^2}{(1+\rho) - 2\beta_1\beta_2}}{1 - \rho} \right]. \quad (8)$$

For a given sample size  $T$  and estimated coefficient  $\hat{\beta}_1 = \bar{\beta}_1$ , this statistic is minimized at  $\hat{\beta}_2 = (1 + \rho)\bar{\beta}_1$ . Since a low value of the statistic implies less evidence against the null, this result means that we not only expect a nonzero  $\hat{\beta}_2$  under the null but that it should be of a magnitude greater than the  $\hat{\beta}_1$  estimate. In fact, for a highly persistent regressor, the Wald statistic is minimized when the 2-period coefficient is almost double the one-period coefficient. Of course, the denominator of the test statistic goes to zero as the autocorrelation approaches 1, so even small deviations from the predicted pattern under the null may generate rejections if the regressor is sufficiently persistent.

These results provide important clues in searching for powerful tests against the null of no predictability. If the alternative hypothesis does not imply coefficient estimates that increase at the same rate across horizons or that are not as heavily tied to the predictive variable's persistence, one can find evidence of predictability even with modestly sized coefficients. But the fact that the no predictability null and the standard ARMA predictive model imply similar coefficient patterns (and thus low power) does not mean the null is false.

Treating the individual coefficient estimates separately in a joint setting can lead to very misleading conclusions. The null hypothesis of no predictability as described by the Wald Test is most supported in the data when we observe monotonically increasing/decreasing coefficient estimates that can be described by the horizon and persistence of the predictive variable. This is the exact pattern documented in the original Fama and French (1988a) and Campbell and Shiller (1988) articles. The relation between short and long horizons under the null of no predictability

<sup>7</sup> For other examples of joint tests in the predictability framework, see, for example, Richardson and Smith (1991), Hodrick (1992) and Ang and Bekaert (2005), among others.

is especially damaging given the weak evidence of predictability at short horizons and also in the context of the previously mentioned data snooping arguments [e.g., Foster, Smith, and Whaley (1997)] and small sample bias [Stambaugh (1999)], both of which suggest that short-horizon significance is overstated.

#### 1.4 Simulation evidence

The theoretical results in Sections 1.2 and 1.3 are based on asymptotic properties of fixed-horizon estimators. *A priori* there is reason to be wary of these results in small samples, particularly because of the considerable evidence of a bias in the coefficient estimators and of nonnormality as discussed in Section 1.1. Therefore, it is useful to evaluate the small sample properties of the estimators in general, and the patterns in sampling error across equations in particular. Previewing the results to come, the basic tenet of Equations (2) and (3), namely, the dependence across equations, carries through to small samples.

We simulate 75 years of annual data under the assumption of no predictability and an AR(1) process on  $X_t$ ,

$$\begin{aligned} R_{t,t+1} &= \varepsilon_{t,t+1} \\ X_{t+1} &= \rho X_t + u_{t,t+1} \end{aligned} \quad (9)$$

and we estimate the model in Equation (1) for 1- to 5-year horizons. The AR parameter  $\rho$ , the standard deviations of  $u_{t,t+1}$  and  $\varepsilon_{t,t+1}$ ,  $\sigma_u$  and  $\sigma_\varepsilon$ , and the correlation between  $\varepsilon_{t,t+1}$  and  $u_{t,t+1}$ ,  $\sigma_{\varepsilon u}$ , are chosen to match the data.<sup>8</sup> The simulations involve 100,000 replications each.

Table 1(A) reports the simulated correlation matrix of the multiple-horizon estimators. Consistent with the analytical calculations in Section 1.2, the correlations tend to be high, even for the most distant horizons. The simulated correlations between the 1-year and 2- to 5-year horizon estimators are 0.966, 0.926, 0.885, and 0.843, respectively, showing that the correlation calculations under the fixed-horizon asymptotics hold in small samples. Thus, the estimators' almost perfect cross-correlation leads to little independent information across equations, and the sampling error that is surely present in small samples shows up in every equation in Equation (1).

As shown in Section 1.2, persistence (i.e.,  $\rho$ ) is an important determinant of the magnitude of the correlation matrix of the multiple-horizon estimators. Figure 1(A) plots the correlation between the 1-year and 2- to 5-year horizon estimators for values  $\rho = 0.953, 0.750, 0.500, 0.250$ , and

<sup>8</sup> Specifically, for the regression of annual stock returns on the most commonly used predictive variable, namely, dividend yields, we estimate  $\rho = 0.953$ ,  $\sigma_\varepsilon = 0.202$ ,  $\sigma_u = 0.154$  and  $\sigma_{\varepsilon u} = -0.712$ . While the magnitudes of  $\sigma_u$  and  $\sigma_\varepsilon$  do not matter, this is not true for either the persistence variable  $\rho$  [Boudoukh and Richardson (1994)] or the correlation  $\sigma_{\varepsilon u}$  [e.g., Stambaugh (1999)]. Thus, we also investigate different values for these parameters.

**Table 1**  
**Distribution of coefficient estimates and test statistics**

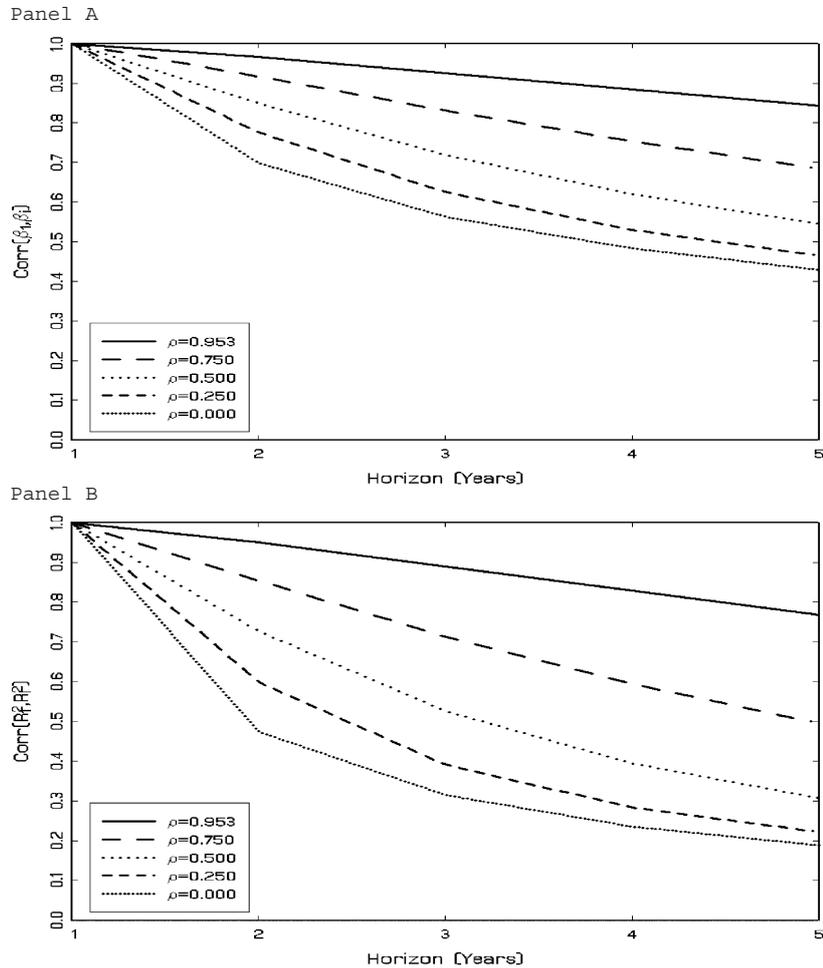
Panel A:  $\sigma_{\varepsilon u} = -0.712$

Coefficient estimates							
Horizon	Mean	SD	Median	Correlations			
				Horizon			
				2	3	4	5
1	0.055	0.076	0.043	0.966	0.926	0.885	0.843
2	0.106	0.143	0.085		0.980	0.946	0.909
3	0.153	0.203	0.126			0.985	0.957
4	0.196	0.257	0.165				0.988
5	0.235	0.307	0.203				
% monotonic		66.02					
Test statistics							
	Mean	SD	Median	Size			
				10%	5%	1%	
Wald	6.227	3.901	5.469	18.507	10.645	3.015	
<i>p</i> -value	0.403	0.288	0.361				

Panel B:  $\sigma_{\varepsilon u} = 0$

Coefficient estimates							
Horizon	Mean	SD	Median	Correlations			
				Horizon			
				2	3	4	5
1	0.000	0.070	0.000	0.960	0.913	0.867	0.823
2	0.000	0.133	0.001		0.977	0.940	0.900
3	0.001	0.194	0.001			0.984	0.954
4	0.001	0.251	0.002				0.988
5	0.000	0.305	0.001				
% monotonic		57.30					
Test statistics							
	Mean	SD	Median	Size			
				10%	5%	1%	
Wald	5.949	3.876	5.142	16.813	9.684	2.773	
<i>p</i> -value	0.429	0.294	0.399				

Panel A reports the mean, standard deviation, and median of the coefficient estimates from the predictive regression (Equation (1)), and the correlations between these estimates for horizons of 1–5 years across 100,000 simulations. “Percentage monotonic” is the percentage of the simulations that produce coefficients that are monotonic in the horizon. Panel A also reports the mean, standard deviation, and median of the joint Wald test statistic (across horizons), the associated *p*-values, and the percentage of statistics that reject the null hypothesis of no predictability at the 10, 5 and 1% levels. There are 75 observations for each simulation, and simulations are performed under the null hypothesis of no predictability using the parameters  $\rho = 0.953$ ,  $\sigma_{\varepsilon} = 0.212$ ,  $\sigma_u = 0.154$ ,  $\sigma_{\varepsilon u} = -0.712$ . Panel B reports the same statistics for  $\sigma_{\varepsilon u} = 0$  (all other simulation parameters are the same as in Panel A).



**Figure 1**  
**Cross-horizon correlations between coefficient estimates and  $R^2$ s**  
 Panel A plots the correlation between the coefficient estimate at the 1-year horizon and those at the 2- to 5-year horizons from the predictive regression (Equation (1)) across 100,000 simulations for different values of  $\rho$  (the autocorrelation of the predictor variable). There are 75 observations for each simulation, and simulations are performed under the null hypothesis of no predictability using the parameters  $\sigma_\varepsilon = 0.212$ ,  $\sigma_u = 0.154$ ,  $\sigma_{\varepsilon u} = -0.712$ . Panel B plots the analogous correlations for the predictive regression  $R^2$ s.

0.000. Consistent with the asymptotic theory, the correlations decrease as  $\rho$  falls. The drop-off can be quite large as the horizon increases. As a function of the above  $\rho$  values, the 1- and 2-year estimators have correlations of 0.966, 0.917, 0.849, 0.776, and 0.698, respectively, and the 1- and 5-year estimators have correlations of 0.843, 0.684, 0.544, 0.465, and 0.429. Even when the predictive variable has no persistence, the correlation can still be

quite high due to the overlapping information across the multiple-horizon returns.

However, the staggering result in Table 1(A) is that 66% of all the replications produce estimates that are monotonic in the horizon. That is, almost two-thirds of the time, the data produce coefficients increasing or decreasing with the horizon, coinciding with the predictions from the asymptotic theory. To understand how unlikely monotonicity is, suppose that the five different multiple-horizon estimators were IID. In this setting, the probability of a monotonic relation is 0.83%, approximately  $\frac{1}{78^{\text{th}}}$  of the true probability for the multiple-horizon estimators. Even with overlapping horizons, monotonicity drops sharply as  $\rho$  falls, that is, from 66% to 37%, 20%, 11%, and 6% for  $\rho = 0.750, 0.500, 0.250,$  and  $0.000$ , respectively. This result further highlights the importance of persistence in the predictive variable for generating these patterns.

One possible explanation for this finding is that the small sample bias increases with the horizon [e.g., Stambaugh (1999), Goetzmann and Jorion (1993), and Kim and Nelson (1993)]. Table 1(A) confirms this pattern, with the means of the 1- to 5-year coefficients equal to 0.055, 0.106, 0.153, 0.196, and 0.235, respectively. To investigate whether the monotonicity is due to this bias, Table 1(B) duplicates Table 1(A) under the assumption that  $\sigma_{\varepsilon u} = 0$ . For this value, the small sample bias is theoretically zero, and the estimates are unbiased in our simulations. Interestingly, the monotonicity falls only slightly, to 57%. Furthermore, Table 1(B) shows that the correlation matrix across the multiple-horizon estimators is virtually identical to that in Table 1(A). Thus, the monotonicity is driven by the almost perfect correlation across the estimators and the increasing horizon, not by the small sample bias.

As described in Section 1.1, much of the literature has argued for predictability by focusing on the increase in the coefficient estimates as a function of the horizon. Both theoretically and in simulation, we show that this result is expected under the null hypothesis of no predictability. An alternative measure of predictability also considered in the literature is the magnitude and pattern of  $R^2$ s across horizons. While the  $R^2$  is linked to the coefficient estimate, it is nevertheless a different statistic of the data. Table 2(A) reports the simulated correlation matrix of the multiple-horizon  $R^2$ s as well as their means, medians, standard deviations, and monotonicity properties.

Similar to Table 1(A), the  $R^2$ s are all highly correlated across horizons. For example, the simulated correlations between the 1-year and 2- to 5-year horizon  $R^2$ s are 0.949, 0.889, 0.828, and 0.767, respectively. This degree of correlation leads to  $R^2$ s that are monotonic in the horizon 52% of the time under the null hypothesis—the exact pattern documented in the literature. This result is not due to the Stambaugh (1999) small sample bias, as both the degree of correlation and monotonicity also

**Table 2**  
Distribution of  $R^2$ s

Panel A:  $\sigma_{\varepsilon u} = -0.712$

Horizon	Mean	SD	Median	Correlations			
				Horizon			
				2	3	4	5
1	1.833	2.378	0.918	0.949	0.889	0.828	0.767
2	3.469	4.348	1.816		0.969	0.918	0.861
3	4.966	6.041	2.665			0.977	0.933
4	6.337	7.525	3.454				0.981
5	7.600	8.837	4.259				
% monotonic		52.21					

Panel B:  $\sigma_{\varepsilon u} = 0$

Horizon	Mean	SD	Median	Correlations			
				Horizon			
				2	3	4	5
1	1.345	1.861	0.618	0.927	0.846	0.768	0.696
2	2.525	3.400	1.203		0.957	0.892	0.821
3	3.614	4.771	1.746			0.969	0.914
4	4.626	5.995	2.280				0.976
5	5.574	7.099	2.790				
% monotonic		42.58					

Panel A reports the mean, standard deviation, and median of the  $R^2$ s from the predictive regression (Equation (1)) and the correlations between them for horizons of 1–5 years across 100,000 simulations. “Percentage monotonic” is the percentage of the simulations that produce  $R^2$ s that are monotonic in the horizon. There are 75 observations for each simulation, and simulations are performed under the null hypothesis of no predictability using the parameters  $\rho = 0.953$ ,  $\sigma_{\varepsilon} = 0.212$ ,  $\sigma_u = 0.154$ ,  $\sigma_{\varepsilon u} = -0.712$ . Panel B reports the same statistics for  $\sigma_{\varepsilon u} = 0$  (all other simulation parameters are the same as in Panel A).

appear in the simulated data without the bias (Table 2(B), where the cross-equation correlation is zero). Also, analogous to the evidence for the multiple-horizon coefficient estimators, the degree of cross-correlation and monotonicity depends crucially on the level of persistence  $\rho$  of the predictive variable.

Figures 1(A) and (B) show the correlation coefficients between the 1- and the  $k$ -period  $\beta$  estimates and  $R^2$ s. The correlations are plotted for different persistence parameters, and the figures illustrate both the monotonicity and near linearity one would expect and the dependence of this effect on the persistence parameter.

The theoretical calculations of Section 1.2 imply an even stronger condition than monotonicity. For  $\rho$  close to 1, the coefficients and  $R^2$ s should increase one-for-one with the horizon under the null hypothesis.

**Table 3**  
**Distribution of coefficient estimate and  $R^2$  cross-horizon ratios**

Panel A:  $\sigma_{\varepsilon U} = -0.712$

Horizon	Coefficient estimate ratios				$R^2$ ratios			
	Mean	SD	Median	# of sim.	Mean	SD	Median	# of sim.
2	1.934	0.874	1.919	88,495	1.957	0.813	1.875	62,126
3	2.798	1.894	2.739	88,495	2.880	1.726	2.612	62,126
4	3.592	3.056	3.472	88,495	3.766	2.744	3.237	62,126
5	4.318	4.326	4.139	88,495	4.612	3.821	3.785	62,126
% monotonic		70.38		% monotonic		60.40		

Panel B:  $\sigma_{\varepsilon U} = 0$

Horizon	Coefficient estimate ratios				$R^2$ ratios			
	Mean	SD	Median	# of sim.	Mean	SD	Median	# of sim.
2	1.872	1.154	1.887	87,058	1.905	0.959	1.783	54,599
3	2.620	2.426	2.665	87,058	2.756	1.987	2.400	54,599
4	3.269	3.846	3.350	87,058	3.552	3.082	2.887	54,599
5	3.835	5.357	3.945	87,058	4.299	4.206	3.241	54,599
% monotonic		61.27		% monotonic		49.00		

Panel A reports the mean, standard deviation, and median of the coefficient estimate and  $R^2$  ratios (i.e.,  $\hat{\beta}_i/\hat{\beta}_1$  and  $R_i^2/R_1^2$ ,  $i = 2, \dots, 5$ ) from the predictive regression (Equation (1)) across the simulations out of the 100,000 for which  $\hat{\beta}_1 > 0.01$  or  $R_1^2 > 0.5\%$ , respectively. “Percentage monotonic” is the percentage of these simulations that produce coefficient estimates and  $R^2$ s that are monotonic in the horizon. There are 75 observations for each simulation, and simulations are performed under the null hypothesis of no predictability using the parameters  $\rho = 0.953$ ,  $\sigma_\varepsilon = 0.212$ ,  $\sigma_u = 0.154$ ,  $\sigma_{\varepsilon U} = -0.712$ . Panel B reports the same statistics for  $\sigma_{\varepsilon U} = 0$  (all other simulation parameters are the same as in Panel A).

Because this is the typical pattern found in U.S. data, it seems worthwhile to investigate this implication through a simulation under the null hypothesis of no predictability. We examine the ratios of the 2- to 5-year coefficient and  $R^2$  estimates to the 1-year estimates. Since there are numerical issues when using denominators close to zero, we run the analysis under the condition that the 1-year estimate have an absolute value greater than 0.01 or an  $R^2$  greater than 0.5%. Approximately 88% and 62% of the simulations respectively satisfy these criteria.

Table 3(A) contains the results. As predicted by the theory, the mean ratios of the estimates are 1.93, 2.80, 3.59, and 4.32 for the 2-, 3-, 4-, and 5-year horizons, respectively. The  $R^2$ s are equally dramatic, with corresponding ratios of 1.96, 2.88, 3.77, and 4.61.<sup>9</sup> Note that these simulations are performed under the null hypothesis of no predictability. The  $\beta$ s are zero, but the other parameters are calibrated to match the joint

<sup>9</sup> Similar to the earlier tables, Table 3(b) shows that these findings are not due to the Stambaugh bias and hold equally well for  $\sigma_{\varepsilon U} = 0$ .

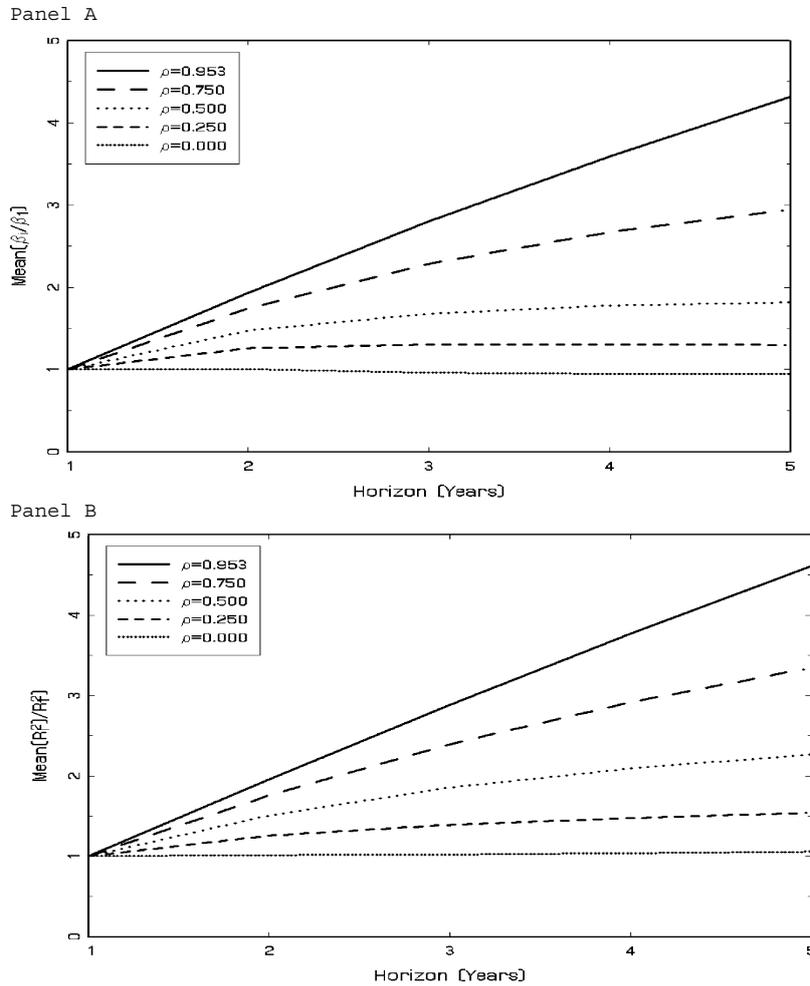
distribution of stock returns and dividend yields in the data. How do these results compare with the estimated coefficients and  $R^2$ s from the actual data? In the data, the ratios for the 2-, 3-, 4-, and 5-year horizons are 1.96, 2.98, 3.53, and 3.99 for the  $\beta$  estimates, and 1.85, 3.07, 3.51, and 4.02 for the  $R^2$ s. The similarities are startling.

Figure 2(A) and (B) plot the ratios as a function of the persistence parameter  $\rho$ . For large  $\rho$ , both the coefficient estimates and  $R^2$ s increase linearly with the horizon, with fairly steep slopes (albeit not quite one-for-one). As persistence drops off, the slope diminishes dramatically. For  $\rho = 0$ , the ratio plot is actually flat. Nevertheless, given the high persistence of the predictive variables used in practice, the more relevant ratios would be those corresponding to steep slopes. These graphs show the mean of the ratio; however, understanding the full distribution allows us to examine whether the actual estimates fall within the empirical null distributions.

To better understand the statistical likelihood of the observed evidence in light of the distribution of the various relevant coefficients under the null hypothesis, Figures 3(A) and (B) show box plots of the distribution of the multiple-horizon coefficient estimates and  $R^2$ s conditional on the 1-year coefficient estimate and  $R^2$  being close to the actual values (i.e.,  $\hat{\beta} = 0.131$  and  $R^2 = 5.16\%$ , Table 4). The box plots show the median, the 25th and 75th percentiles, and the more extreme 10th and 90th percentiles of the distribution. Several observations are in order. First, consistent with Figure 2(A) and (B), the percentiles linearly increase at a fairly steep rate. Second, the actual values of the coefficients and  $R^2$ s from the data (marked as diamonds in the graph) lie uniformly between the 25th and 75th percentiles. Given some amount of sampling error, the hypothesis of no predictability produces precisely the pattern one would expect in the coefficients under the alternative hypothesis. Because the sample sizes are relatively small, the presence of sampling error is almost guaranteed. Third, the plots show that what matters is the magnitude of the coefficient at short horizons. In the voluminous literature on stock return predictability in finance, researchers have generally not considered the short-horizon evidence to be that remarkable.

## 2. Empirical Evidence

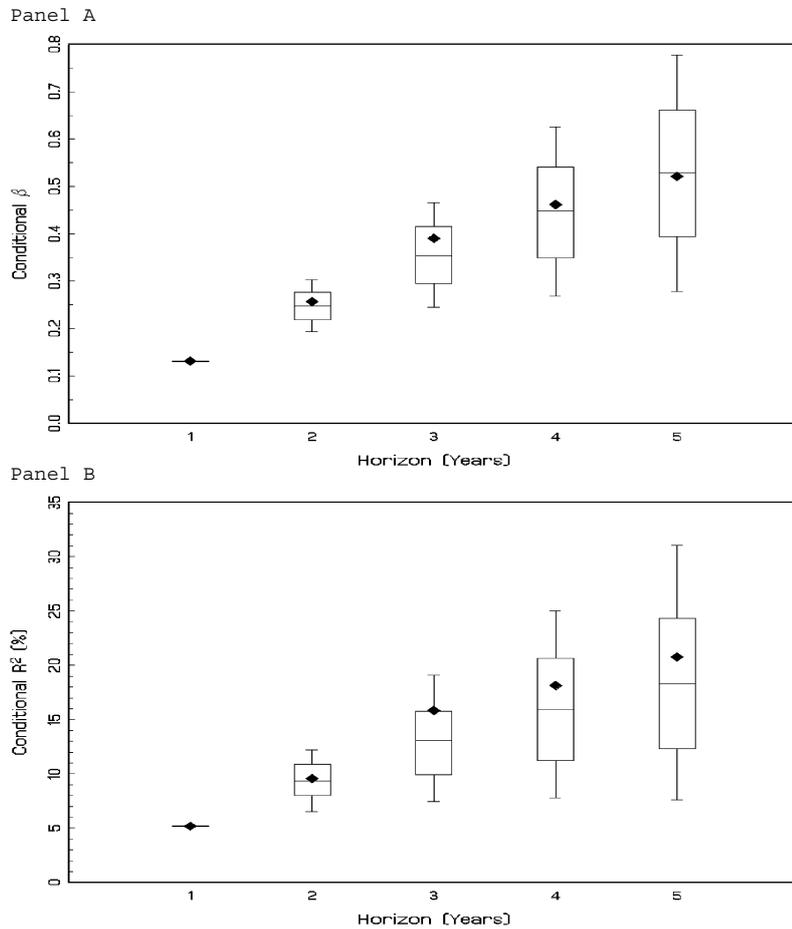
The theory and corresponding simulation evidence in Section 1 suggest that it will be very difficult to distinguish between the null hypothesis of no predictability and alternative models of time-varying expected returns that involve persistent autoregressive processes. The reason is that sampling error produces virtually identical patterns in both  $R^2$ s and coefficients across horizons. However, this finding does not necessarily imply that joint tests will not distinguish the null from other alternatives. Recall that the null hypothesis implies highly correlated regression coefficient



**Figure 2**  
**Mean coefficient estimate and  $R^2$  cross-horizon ratios**  
 Panel A plots the mean coefficient estimate ratios (i.e.,  $\hat{\beta}_i/\hat{\beta}_1, i = 2, \dots, 5$ ) from the predictive regression (Equation (1)) across the simulations out of the 100,000 for which  $|\hat{\beta}_1| > 0.01$  for different values of  $\rho$  (the autocorrelation of the predictor variable). There are 75 observations for each simulation, and simulations are performed under the null hypothesis of no predictability using the parameters  $\sigma_\varepsilon = 0.212$ ,  $\sigma_u = 0.154$ ,  $\sigma_{\varepsilon u} = -0.712$ . Panel B plots the means of the analogous  $R^2$  ratios (i.e.,  $R_i^2/R_1^2, i = 2, \dots, 5$ ) for simulations with or  $R_1^2 > 0.5\%$ .

estimators, which induce the coefficient pattern. Even with unremarkable coefficient estimators, yet nonconforming coefficient patterns, one might find strong evidence against the null hypothesis of no predictability.

There are few examples of an empirically-based critique of long-horizon predictability, exceptions being the recent article by Ang and Bekaert



**Figure 3**  
**Conditional distribution of coefficient estimates and  $R^2$ s**  
 Panel A provides a box plot of the simulated distributions of the coefficient estimates for horizons 2- to 5-years from the predictive regression (Equation (1)) for the 971 out of 100,000 simulations for which  $0.115 < \hat{\beta}_1 < 0.119$ . The boxes show the median, 25th/75th percentiles, and 10th/90th percentiles. The diamonds mark the actual coefficient estimates from the first regression in Table 4. There are 75 observations for each simulation, and simulations are performed under the null hypothesis of no predictability using the parameters  $\rho = 0.953$ ,  $\sigma_\varepsilon = 0.212$ ,  $\sigma_u = 0.154$ ,  $\sigma_{\varepsilon u} = -0.712$ . Panel B plots the analogous simulated distributions for the predictive regression  $R^2$ s for the 899 simulations for which  $4.215\% < R_1^2 < 4.414\%$  and the corresponding actual  $R^2$ s.

(2005), and previous work by Goetzmann and Jorion (1993) and Kim and Nelson (1993). In this section, we look at a number of commonly used variables to test the predictability of stock returns. For stock returns, we use the excess return on the value-weighted (VW) Center for Research in Security Prices (CRSP) portfolio, where excess returns are calculated

**Table 4**  
Coefficient estimates and  $R^2$ s from predictive regressions

	Horizon					Wald
	1	2	3	4	5	
<b>Log dividend yield, CRSP VW</b>						
$\hat{\beta}$	0.131	0.257	0.390	0.461	0.521	7.576
Std. err.	0.067	0.130	0.191	0.249	0.306	
Asym. $p$ -value	0.025	0.025	0.021	0.032	0.044	0.181
Sim. $p$ -value	0.148	0.142	0.125	0.150	0.172	0.293
$R^2$	5.164	9.551	15.836	18.143	20.756	
<b>Log payout yield, CRSP VW, cash flow</b>						
$\hat{\beta}$	0.214	0.401	0.567	0.657	0.736	7.840
Std. err.	0.085	0.162	0.235	0.304	0.370	
Asym. $p$ -value	0.006	0.007	0.008	0.015	0.023	0.165
Sim. $p$ -value	0.046	0.045	0.044	0.059	0.072	0.211
$R^2$	8.664	14.530	20.912	22.997	25.829	
<b>Log payout yield, CRSP VW, Treasury stock</b>						
$\hat{\beta}$	0.188	0.354	0.510	0.601	0.682	7.309
Std. err.	0.078	0.152	0.221	0.286	0.350	
Asym. $p$ -value	0.008	0.010	0.010	0.018	0.026	0.199
Sim. $p$ -value	0.072	0.069	0.066	0.082	0.096	0.270
$R^2$	7.729	13.213	19.714	22.387	25.827	
<b>Log net payout yield, CRSP VW, cash flow</b>						
$\hat{\beta}$	0.718	1.321	1.536	1.537	1.512	19.024
Std. err.	0.173	0.315	0.431	0.528	0.616	
Asym. $p$ -value	0.000	0.000	0.000	0.002	0.007	0.002
Sim. $p$ -value	0.000	0.000	0.001	0.004	0.012	0.001
$R^2$	23.399	37.990	36.887	30.253	26.247	
<b>Log earnings yield, S&amp;P 500</b>						
$\hat{\beta}$	0.101	0.228	0.328	0.383	0.380	5.175
Std. err.	0.064	0.120	0.171	0.218	0.262	
Asym. $p$ -value	0.057	0.028	0.028	0.040	0.073	0.395
Sim. $p$ -value	0.125	0.073	0.066	0.081	0.129	0.430
$R^2$	3.334	8.065	11.757	13.373	11.798	

at a monthly frequency using the 1-month T-bill rate from the CRSP Fama risk-free rate file. For predictors, we use the log dividend yield on the CRSPVW index, three other payout yields adjusted for repurchases and new equity issues, the log earnings yield on the Standard & Poor's (S&P500), the default spread between Baa and Aaa yields, the term spread between long-term government bond yields and Treasury-bill yields, the log book-to-market ratio, the aggregate equity share of new issuances, and the 1-month Treasury-bill yield.<sup>10</sup>

The regression analysis corresponds to Equation (1), and covers return horizons of 1–5 years over the period 1926–2004. We use the same number of observations for each horizon; therefore, the predictor variables span

<sup>10</sup> See Boudoukh, Michaely, Richardson, and Roberts (2005) for a detailed description of the various measures of payout yield. The data for the first 4 variables are available on Michael Roberts' website <http://www.finance.wharton.upenn.edu/mrrobert/public.html/Research/Data>. See Goyal and Welch (2005) for details on variables 5–8. We thank Amit Goyal for graciously providing the data. See Baker and Wurgler (2000) for a description of the equity share of new issuances. The data are available on Jeff Wurgler's website <http://pages.stern.nyu.edu/~jwurgler/>. The 1-month Treasury-bill yield comes from the CRSP Fama risk-free rate file.

**Table 4**  
**(Continued)**

	Horizon					Wald
	1	2	3	4	5	
Default yield spread						
$\hat{\beta}$	1.372	4.961	7.111	9.982	12.512	3.335
Std. err.	2.864	5.420	7.734	9.825	11.759	
Asym. $p$ -value	0.316	0.180	0.179	0.155	0.144	0.648
Sim. $p$ -value	0.429	0.278	0.280	0.251	0.237	0.690
$R^2$	0.306	1.911	2.770	4.559	6.417	
Term yield spread						
$\hat{\beta}$	2.663	3.715	5.860	9.350	11.336	7.082
Std. err.	1.763	3.157	4.260	5.136	5.853	
Asym. $p$ -value	0.065	0.120	0.084	0.034	0.026	0.215
Sim. $p$ -value	0.077	0.133	0.100	0.048	0.043	0.230
$R^2$	3.041	2.829	4.966	10.560	13.905	
Log book-to-market ratio						
$\hat{\beta}$	0.086	0.187	0.289	0.358	0.384	5.841
Std. err.	0.052	0.100	0.146	0.189	0.229	
Asym. $p$ -value	0.049	0.031	0.024	0.029	0.047	0.322
Sim. $p$ -value	0.225	0.180	0.155	0.164	0.208	0.441
$R^2$	3.665	8.295	13.988	18.023	18.520	
Equity share of new issuances						
$\hat{\beta}$	-0.741	-1.181	-1.311	-1.351	-1.189	16.161
Std. err.	0.216	0.352	0.461	0.552	0.652	
Asym. $p$ -value	0.000	0.000	0.002	0.007	0.034	0.006
Sim. $p$ -value	0.001	0.001	0.005	0.012	0.039	0.005
$R^2$	16.126	20.103	17.271	14.976	10.831	
Risk-free rate						
$\hat{\beta}$	-1.287	-1.812	-2.911	-4.234	-5.165	9.776
Std. err.	0.842	1.644	2.420	3.176	3.918	
Asym. $p$ -value	0.063	0.135	0.114	0.091	0.094	0.082
Sim. $p$ -value	0.075	0.141	0.119	0.094	0.094	0.145
$R^2$	3.112	2.946	5.367	9.485	12.646	

The table reports results from the regression of 1- to 5-year CRSP (Center for Research in Security Prices) value-weighted (VW) returns on various lagged predictor variables (Equation (1)) for the period 1926–2004 (75 observations).  $\hat{\beta}$  is the estimated coefficient, with associated asymptotic standard error (equation (3)),  $p$ -value under the null hypothesis of no predictability, and the asymptotic Wald test and  $p$ -value for the joint hypothesis of no predictability across horizons. The table also reports simulated  $p$ -values (100,000 simulations) for both the individual coefficients and the Wald test. There are 75 observations for each simulation, and simulations are performed under the null hypothesis of no predictability using parameters estimated from the data.

the period 1925–1999 (75 observations) when available.<sup>11</sup> For each set of multiple-horizon regressions, we calculate the coefficient, its analytical standard error (using Equation (2)), its asymptotic  $p$ -value, and its simulated  $p$ -value under an AR(1) with matching parameters.<sup>12</sup> The

<sup>11</sup> The four payout yield series start in 1926 (74 observations) and the equity share series starts in 1927 (73 observations).

<sup>12</sup> Because the equations involve overlapping observations across multiple horizons, small sample adjustments for coefficient estimators and standard errors [e.g., Amihud and Hurvich (2004) and Amihud, Hurvich, and Wang (2005)] are no longer strictly valid. As developing methods for our particular regression system lies outside the scope of this article, we rely on simulated  $p$ -values as a correction for both the correlation [e.g., Stambaugh (1999)] and long-horizon [e.g., Valkanov (2003)] biases.

AR(1) coefficient used in the simulations is the estimated first-order autocorrelation, corrected for the small sample bias [Kendall (1954)],

$$\hat{\rho}_{1C} = \hat{\rho}_1 + \frac{1 + 3\hat{\rho}_1}{T}. \quad (10)$$

In addition, we conduct a joint Wald test across the equations, reporting both asymptotic and simulated  $p$ -values. Throughout, asymptotic standard errors,  $p$ -values, and test statistics are calculated using the uncorrected sample autocorrelation function.<sup>13</sup> The results are reported in Table 4.

Most of the series show the much-cited pattern of increasing coefficient estimates and corresponding  $R^2$ s. For the dividend yield, the payout yield including total repurchases, the payout yield including treasury stock-adjusted repurchases (all on the CRSP VW index), the earnings yields on the S&P500, the default spread, the term spread, the book-to-market ratio, and the risk-free rate the increases in  $R^2$  from the 1-year to the 5-year horizon are 5.16–20.76%, 8.66–25.83%, 7.73–25.83%, 3.33–11.80%, 0.31–6.42%, 3.04–13.90%, 3.66–18.52%, and 3.11–12.65%, respectively. However, the (corrected) persistence levels of the associated variables are 95.3%, 88.7%, 91.9%, 79.1%, 83.8%, 64.2%, 93.4%, and 95.7%, respectively (Table 5). It should not be surprising that many of the series have significant coefficients using asymptotic  $p$ -values across most of the horizons. Under the null hypothesis, the regressions at each horizon are virtually the same.

Table 5 is an alternative representation of the results in Table 4, i.e., the ratios of the coefficient estimates and  $R^2$ s across horizons. For the series cited above (except for the default spread), the ratios for both quantities are similar to the simulated ratios under the null hypothesis of no predictability. In all cases, the ratios (and therefore the underlying coefficient estimates and  $R^2$ s) increase with the horizon. Thus, the finding that some of the 1-year regressions are significant, and that the same variables produce virtually identical patterns at longer horizons, is actually evidence that the annual regression results are due to sampling error.<sup>14</sup> The joint tests confirm this phenomenon by generally producing higher  $p$ -values, for example 0.18, 0.16 and 0.20 for the three payout yield variables on the CRSP VW index, 0.39 for the earnings yield on the S&P500, 0.65 for the default spread, 0.32 for the term spread, 0.32 for the book-to-market

<sup>13</sup> Using the uncorrected sample autocorrelation function has the advantage of generating invertible covariance matrices in every dataset and simulation, which would not be true for either corrected sample autocorrelations or autocorrelations estimated via regressions.

<sup>14</sup> This conclusion has even greater support once the researcher takes into account the data-snooping arguments of Foster, Smith, and Whaley (1997).

**Table 5**  
Autocorrelation estimates and coefficient estimate and  $R^2$  ratios from predictive regressions

		Horizon				$\hat{\rho}_{1C}$
		2	3	4	5	
ln (D/P) (CRSP VW)	$\hat{\rho}_{i-1}$	0.901	0.780	0.687	0.637	0.953
	$\hat{\beta}_i/\hat{\beta}_1$	1.962	2.982	3.527	3.986	
	$R_i^2/R_1^2$	1.850	3.067	3.514	4.020	
ln (payout/P) (CRSP VW, CF)	$\hat{\rho}_{i-1}$	0.837	0.674	0.574	0.508	0.887
	$\hat{\beta}_i/\hat{\beta}_1$	1.869	2.645	3.065	3.432	
	$R_i^2/R_1^2$	1.677	2.414	2.654	2.981	
Ln (payout/P) (CRSP VW, TS)	$\hat{\rho}_{i-1}$	0.867	0.721	0.618	0.567	0.919
	$\hat{\beta}_i/\hat{\beta}_1$	1.887	2.719	3.202	3.634	
	$R_i^2/R_1^2$	1.710	2.551	2.897	3.342	
ln (net payout/P) (CRSP VW, CF)	$\hat{\rho}_{i-1}$	0.670	0.280	0.108	0.128	0.713
	$\hat{\beta}_i/\hat{\beta}_1$	1.839	2.138	2.139	2.105	
	$R_i^2/R_1^2$	1.624	1.576	1.293	1.122	
ln (E/P) (S&P500)	$\hat{\rho}_{i-1}$	0.746	0.565	0.405	0.318	0.791
	$\hat{\beta}_i/\hat{\beta}_1$	2.250	3.234	3.774	3.746	
	$R_i^2/R_1^2$	2.419	3.527	4.011	3.539	
Default spread	$\hat{\rho}_{i-1}$	0.790	0.564	0.383	0.306	0.838
	$\hat{\beta}_i/\hat{\beta}_1$	3.617	5.184	7.277	9.122	
	$R_i^2/R_1^2$	6.250	9.060	14.912	20.990	
Term spread	$\hat{\rho}_{i-1}$	0.603	0.213	0.008	-0.058	0.642
	$\hat{\beta}_i/\hat{\beta}_1$	1.395	2.201	3.511	4.257	
	$R_i^2/R_1^2$	0.930	1.633	3.472	4.572	
ln (B/M)	$\hat{\rho}_{i-1}$	0.882	0.721	0.580	0.456	0.934
	$\hat{\beta}_i/\hat{\beta}_1$	2.177	3.364	4.179	4.476	
	$R_i^2/R_1^2$	2.263	3.816	4.917	5.053	
Equity share of new issuances	$\hat{\rho}_{i-1}$	0.332	0.116	0.046	0.291	0.360
	$\hat{\beta}_i/\hat{\beta}_1$	1.594	1.771	1.824	1.605	
	$R_i^2/R_1^2$	1.247	1.071	0.929	0.672	
Risk-free rate	$\hat{\rho}_{i-1}$	0.905	0.816	0.759	0.730	0.957
	$\hat{\beta}_i/\hat{\beta}_1$	1.408	2.262	3.290	4.014	
	$R_i^2/R_1^2$	0.947	1.725	3.048	4.064	

The table reports the estimated autocorrelation function ( $\hat{\rho}_{i-1}$ ), the corrected first-order autocorrelation ( $\hat{\rho}_{1C}$ ), the coefficient estimate ratios ( $\hat{\beta}_i/\hat{\beta}_1$ ,  $i = 2, \dots, 5$ ) and the  $R^2$  ratios ( $R_i^2/R_1^2$ ,  $i = 2, \dots, 5$ ) from the regression of 15 year CRSP value-weighted returns on various lagged predictor variables (Equation (1)) for the period 1926–2004.

ratio, and 0.08 for the risk-free rate, the only variable significant at the 10% level.<sup>15</sup>

Several observations illustrate the nature of the joint tests. First, consider the regression results for the dividend yield versus the two payout yield measures on the CRSP VW index. By almost any eyeball measure, the evidence for the payout yields appears to be stronger. All of the horizons produce larger coefficient estimates and  $R^2$ s and lower  $p$ -values. While

<sup>15</sup> Of course, we are testing for predictability in a restrictive, linear, constant coefficient setting. One explanation for the lack of predictive power in these regressions is that the relation is nonstationary [e.g., Jagannathan, McGrattan, and Scherbina (2000) and Lettau and Van Nieuwerburgh (2006)].

four of the five asymptotic  $p$ -values are less than 0.02 for both payout yield measures, none of the coefficients satisfy this criterion for the dividend yield. Nevertheless, the  $p$ -values of the joint tests for the payout yields are similar to that for the dividend yield. Similarly, the individual coefficient  $p$ -values and corresponding  $R^2$ s for the risk-free rate, the one marginally significant variable out of the series cited above under the asymptotic cross-horizon test, look less impressive if anything than those for the other series. Yet the significance level of the joint test is much higher.<sup>16</sup>

What explains these apparently anomalous results? The dividend yield and the risk-free rate have the highest autocorrelations among all the variables. Under the null, the coefficient estimates across horizons are extremely highly correlated. For example, for both variables, the correlations between coefficient estimates at adjacent horizons range between 0.96 and 0.99 in simulations. Thus, even small deviations in the pattern in the coefficients from that implied by the estimated autocorrelation function are statistically significant. This result illustrates the power of the joint test to uncover seemingly innocuous differences across horizons.

Second, the simulated  $p$ -values in general show much less significance for both the individual and joint tests. For example, the risk-free rate is no longer significant at the 10% level. This mirrors the small sample findings of Goetzmann and Jorion (1993), Kim and Nelson (1993), and Valkanov (2003). As Table 1(A) and (B) show, the correlation pattern across multiple-horizon estimators is robust to small sample considerations.

Finally, two variables, the net payout yield (i.e., payout yield plus net issuance) and the equity share of new issuances, are strongly significant across horizons as evidenced by Wald statistics with  $p$ -values of 0.00 and 0.01, respectively. These results are consistent with the short-horizon findings of Boudoukh, Michaely, Richardson, and Roberts (2005) and Baker and Wurgler (2000),<sup>17</sup> and show that this predictability is also evident at long horizons. The significance of the joint tests is mainly due to the striking predictive power of these variables at the individual horizons, with both asymptotic and simulated  $p$ -values under 0.01 for all but the longest horizons. Of some interest, however, the simulated  $p$ -values of the joint tests are actually lower than their asymptotic counterparts, which is not the case for any of the other variables. This phenomenon is attributable to the fact that the autocorrelation structure of these variables is not totally consistent with the AR(1)

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<sup>16</sup> In a multivariate regression framework that includes both dividend yields and the short rate, Ang and Bekaert (2005) find that the short rate has predictive power across multiple horizons.

<sup>17</sup> These short-horizon results are not completely uncontroversial. For example, see Butler, Grullon, and Weston (2005) for a critique of Baker and Wurgler (2000) and Baker, Taliaferro, and Wurgler (2006) for a response to this critique.

specification in the simulations (Table 5). For net payout, the sample autocorrelations drop off more quickly than implied by an AR(1), while for the equity share the fourth-order autocorrelation is substantially higher than the autocorrelation at lags 2 and 3. Interestingly, the patterns in the coefficients and  $R^2$ s do not seem to be totally consistent with either the AR(1) specification or the sample autocorrelations, under the null. For example, the coefficient ratios for the equity share are higher than those implied by a variable with such a low autocorrelation, yet the associated  $R^2$  ratios are decreasing rather than increasing. These anomalous patterns also contribute to the significance of the joint test statistics.

As noted above, the simulated  $p$ -values are conditional on the specification of the simulated model in Equation (9), i.e., they are only correct to the extent that the AR(1) model is a good representation of the data. This specification appears to be adequate for the standard predictors, which tend to have high first-order autocorrelations, but is less so for the newer predictors, such as net payout, and particularly the equity share of new issuances. For example, these variables appear to respond more to past returns than is captured by the correlation between the shocks to annual returns and the predictor.<sup>18</sup> This relation between the predictor and lagged returns [referred to as pseudo market timing by Schultz (2003)] generates a bias in exactly the same way as does the mechanical correlation between returns and predictors that are price-scaled [Stambaugh (1999)]. Consequently, we also estimate and simulate processes for the predictor variables that are augmented with lagged returns. For the predictors that we consider, the resulting bias in the coefficient can be up to twice as large as for an AR(1) process, but it is still small in magnitude relative to the estimated coefficients. Moreover, qualitatively all the results we discuss above hold with the more elaborate specification.

### 3. Conclusion

Long-horizon stock return predictability is considered by many to be one of the more important results in the empirical asset pricing literature over the last couple of decades [e.g., see the textbooks of Campbell, Lo, and MacKinlay (1997) and Cochrane (2001)]. The evidence is set forth as a yardstick for theoretical asset pricing models and is slowly penetrating the practitioner community [for two recent examples, see Brennan and Xia (2005) and Asness (2003)].

Long-horizon predictability has also been documented in other markets, which is perhaps not surprising given our analysis. The highly cited work

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<sup>18</sup> We thank the editor, Matt Spiegel, for suggesting this avenue of inquiry.

of Fama and Bliss (1987) and Mark (1995) document results similar in spirit to the ones discussed in this article for bond returns and exchange rates, respectively. Both articles involve highly persistent regressors and document nearly linearly increasing  $\beta$ 's and  $R^2$ s.

In this article, we show that stronger long-horizon results, in the form of higher  $\beta$ 's and increasing  $R^2$ s, present little, if any, independent evidence over and above the short-horizon results for persistent regressors. Under the null hypothesis of no predictability, sampling variation can generate small levels of predictability at short horizons. This result is well known. Our research shows that higher levels of predictability at longer horizons are to be expected as well.

### Appendix A:

Under the null hypothesis of no predictability,  $\beta_1 = \dots = \beta_j = \dots = \beta_J = 0$ , we can write the moment conditions corresponding to the regression system in Equation (1) as

$$E[f_t(\cdot)] = E \begin{pmatrix} (R_{t,t+1} - \alpha_1 + \beta_1 X_t) \\ (R_{t,t+1} - \alpha_1 + \beta_1 X_t)X_t \\ \vdots \\ (R_{t,t+j} - j\alpha_1 + \beta_j X_t)X_t \\ \vdots \\ (R_{t,t+J} - J\alpha_1 + \beta_J X_t)X_t \end{pmatrix} = 0. \quad (\text{A1})$$

Under the assumption of conditional homoskedasticity of the error terms above, one can apply the approach of Richardson and Smith (1991) [see also Boudoukh and Richardson (1994)] to analytically derive the asymptotic distribution of the estimators  $\hat{\beta}' = (\hat{\beta}_1 \dots \hat{\beta}_j \dots \hat{\beta}_J)$ . Applying results from Hansen (1982), the vector of regression coefficients  $\hat{\theta} = (\hat{\alpha}_1 \hat{\beta})'$  has an asymptotic normal distribution with mean  $(\alpha_1 \ 0)'$  and covariance matrix  $[D_0' S_0^{-1} D_0]^{-1}$ , where  $D_0 = E \left[ \frac{\partial f_t}{\partial \theta} \right]$  and  $S_0 = \sum_{l=-\infty}^{+\infty} E[f_t f_{t-l}]$ . Under these assumptions, it is possible to calculate  $D_0$  and  $S_0$  analytically. Specifically,

$$D_0 = \begin{pmatrix} 1 & \mu_X & 0 & \dots & \dots & \dots \\ \mu_X & \mu_X^2 + \sigma_X^2 & 0 & \dots & \dots & \dots \\ \vdots & 0 & \ddots & 0 & \dots & \dots \\ j\mu_X & \vdots & 0 & \mu_X^2 + \sigma_X^2 & 0 & \dots \\ \vdots & \vdots & \vdots & 0 & \ddots & 0 \\ J\mu_X & \vdots & \vdots & \vdots & 0 & \mu_X^2 + \sigma_X^2 \end{pmatrix}, \quad (\text{A2})$$

and



where  $\mu_X$  is the mean of  $X_t$ ,  $\sigma_X^2$  is the unconditional variance of  $X_t$ ,  $\rho_l$  is the  $l^{\text{th}}$  order autocorrelation of  $X_t$ , and  $\sigma_R^2$  is the variance of single period returns  $R_{t,t+1}$ . Using  $D_0$  and  $S_0$  above, and performing the relevant matrix calculations, one gets the result in Equation (2).

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