

MSc. Finance/CLEFIN 2014/2015 Edition

Advanced Tools for Risk Management and Asset Pricing

June 2015 Exam for Non-Attending Students - Solutions

Time Allowed: 120 minutes

Family Name (Surname)	First Name	Student Number (Matr.)

Please answer all questions by choosing the most appropriate alternative and/or by writing your answers in the spaces provided. You need to carefully justify and show your work in the case of "open" questions. There is only one correct answer(s) for each of the multiple choice questions: each selected alternative that is correct will be awarded one point. Only answers explicitly reported in the appropriate box will be considered. No other answers or indications pointing to potential answers will be taken into consideration. In the case of "open" questions, the maximum number of points is indicated.

Question 3. Let X_1 and X_2 be two random variables with marginal F_1 and F_2 respectively.
Then, which of the following statements is FALSE?
\square (A) If for X $_1$ and X $_2$ $\lim_{q\to 1^-} P(X_2 > F_2^\leftarrow(q) X_1 > F_1^\leftarrow(q)) = 0$, then X $_1$ and X $_2$ are
asymptotically independent in the upper tail
\square (B) If for X ₁ and X ₂ $\lim_{q\to 0^+} P(X_2 > F_2^{\leftarrow}(q) X_1 > F_1^{\leftarrow}(q)) = 0$, then X ₁ and X ₂ are
asymptotically independent in the lower tail
\square (C) Tail dependence measures depend only on the copula of X_1 , X_2
\square (D) Measures of extremal dependence between a pair of random variables X_1 and X_2
depend only on the copula of X_1 and X_2
Question 4. Which of the following statements about Copulas is TRUE?
(A) Gaussian copula is asymptotically independent in both tails
(B) Gumbel copula has upper tail dependence
(C) Claiton copula has lower tail dependence
(D) All of the above it TRUE
Question 5. Which of the following statements about Rank Correlations is FALSE?
(A) To compute rank correlations one needs to know the ordering of the sample for each
variable
\square (B) Rank correlations are invariant under strictly increasing transformations
\square (C) Rank correlations take a value of -1 when the variables are comonotonic and the value
1 when the variables are countermonotonic
(D) The sample version of Spearman's Rho can be simply expressed as:
$\rho(X_1, X_2) = \rho(R_1, R_2)$
where R_1 and R_2 are rank variables
Question 6.
1. Write down a definition of Copula and its properties.
2. Consider two standard normal random variables X_1 , X_2 that are jointly normal with
correlation ρ . Write the copula functions for the following values of ρ :
a) $\rho = 0$
b) $\rho = 1$
c) $\rho = 1/2$
d) Write the copula for the random vector (X_1, X_2^3) when $\rho = 1/2$

Question 7. Which of the following statements about base correlations is TRUE?
(A) Typically, base correlation presents a smile
(B) It depends on pairs of detachment points
(C) It is inconsistent across the capital structure but consistent at the level of single
tranche (D) It is inconsistent across the capital structure
Question 8. Which of the following statements about different approaches to price CDOs is false?
(A) The One Factor Gaussian Copula Approach allows for dimensionality reduction in the
calculation of the joint default probability of <i>n</i> names
\square (B) Dynamic(al) Loss Approaches allow to calculate single name sensitivities
(C)Dynamic(al) Loss Approaches are able to capture the phenomenon of clustered
(sector) defaults associated to masses in the far right tail of the loss distribution
(D) The Implied Copula Approach by Hull and White is able to capture the phenomenon of clustered (sector) defaults associated to masses in the far right tail of the loss distribution

Portfolio model is FALSE?
 ☐ (A) It is reliable for any portfolio of loans ☐ (B) It depends on the confidence level ☐ (C) It depends on the first moment of the loss distribution ☐ (D) It is an asymptotic formula
Question 10. Which of the following statements about First Passage Time models is FALSE?
 ☐ (A) Default can occur at any time up to maturity ☐ (B) The Black Cox model does not allow for a flexible CDS calibration ☐ (C) AT1P models always produce reasonable results ☐ (D) Default is described through an endogenous process
Question 11. Which of the following statements about compound correlations is FALSE?
 ☐ (A) Typically, compound correlation presents a smile ☐ (B) It depends on pairs of detachment points ☐ (C) It is inconsistent at the level of single tranche ☐ (D) It is inconsistent across the capital structure
Question 12. Which of the following statements about time homogeneous Poisson processes is FALSE?
 ☐ (A) The probability of having no jumps up to a certain time is an exponential function of minus that time ☐ (B) The probability of having more than one jump in an arbitrarily small time goes to zero faster than time ☐ (C) The probability of having one jump in an arbitrarily small time is exactly the constant appearing in the exponential function ☐ (D) A time homogeneous Poisson process is a unit-jump increasing, right continuous process, with stationary independent increments and zero initial value
Question 13. Which of the following statements about Cox processes is FALSE?
\square (A) The first jump time, transformed through its cumulated intensity $\Lambda(\tau)$, is an exponential random variable independent of the default free information \square (B) The survival probability is given by: $P(\tau > T) = e^{-\Lambda(T)}$ \square (C) Default is described by an exogenous jump process \square (D) Stochastic intensity models do not allow to obtain large levels of option implied volatilities for CDS rates

Question 14. Which of the following statements about credit modeling in a multi-factor set up is FALSE?
 ☐ (A) Sector concentration risk affects also the zero order term in the quantile expansion ☐ (B) The conditional asset correlation takes into account the effects of both sector Concentration and name concentration ☐ (C) Name concentration risk cannot be diversified away ☐ (D) In the case of a large enough, fine-grained, portfolio, losses are primarily driven by the systematic factors
Question 15. Which of the following statements about the Sensitivity Based Approach (SBA) is FALSE?
 ☐ (A) Risk factors and sensitivities are defined by the regulator and must be computed by banks accordingly ☐ (B) Sensitivities are used as inputs into aggregation formulae which are intended to recognize hedging and diversification benefits of positions in different risk factors within an asset class ☐ (C) Vega risk and curvature risk do not apply to instruments that are not subject to optionality ☐ (D) Vega risk is applied to options in the calculation of both SBA for capital and SBA for margin
Question 16. Which of the following statements about Mapping methods for bespoke portfolios is FALSE?
 ☐ (A) Mapping consists in associating to the selected bespoken tranche an equivalent base tranche on a standard (index) portfolio ☐ (B) The correlation used to price the bespoke tranche is taken to be the correlation at the equivalent standard strike ☐ (C) In the ATM method the invariant measure of risk in a tranche is the strike as a fraction of its expected loss ☐ (D) The ATM method works well when taking into account the portfolio dispersion

Question 17. Consider the following formula:

$$Q(\tau_1 < T, \dots, \tau_n < T) = \int \left[\prod_{i=1}^n N\left(\frac{N^{-1}\left(1 - e^{-\Gamma_i(T)}\right) - \sqrt{\rho_i} \ y}{\sqrt{1 - \rho_i}}\right) \right] \varphi(y) dy$$

- 1. What does it represent?
- 2. Under which assumptions has been derived?
- 3. Explain the meaning of the following quantities:

 - $N\left(\frac{N^{-1}(1-e^{-\Gamma_i(T)})-\sqrt{\rho_i}y}{\sqrt{1-\rho_i}}\right)$ $\prod_{i=1}^{n} N\left(\frac{N^{-1}(1-e^{-\Gamma_i(T)})-\sqrt{\rho_i}y}{\sqrt{1-\rho_i}}\right)$
 - φ(y)

 - ρ_i
 Γ_i(T)

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Question 19. Considering the two termsheets below, which of the following statements is plausible:

Bonus Cap A			
Underlying	Fiat		
Maturity	3 Years		
Barrier	70%		
Barrier type	American		

Eur 4 to make a 100% protection possible

(E) None of the above

Bonus Cap B			
Underlying	Fiat		
Maturity	3 Years		
Barrier	60%		
Barrier type	American		

 ☐ (A) Bonus Cap A has a Bonus equal to 114% and Bonus Cap B has a Bonus equal to 118% ☐ (B) Bonus Cap A has a Bonus equal to 109% and Bonus Cap B has a Bonus equal to 105% ☐ (C) Bonus Cap A has a Bonus equal to 107% and Bonus Cap B has a Bonus equal to 107% ☐ (D) Bonus Cap A has a Bonus equal to 97% and Bonus Cap B has a Bonus equal to 94%
(b) Bonus cup it has a Bonus equal to 577,0 and Bonus cup B has a Bonus equal to 517,0
Question 20. You are structuring an Equity Protection certificate with 100% capital
protection; the Zero Coupon Bond costs Eur 96. An ATM call option on the FTSE MIB index costs 6 Euro. Because you would like your product to offer 100% participation to any
potential appreciation of the underlying, which strategy of selection of an underlying different
from the FTSE MIB index would you consider?
(A) I shall not need any alternative selection of the underlying asset because I can already offer 100% participation to any potential appreciation of the underlying
\square (B) I will be looking for an underlying asset with lower volatility and dividend yield than
the FTSE MIB so that the option will be cheaper to try and aim at an option cost of Eur 6 to
make a 100% protection possible
(C) I will be looking for an underlying asset with higher volatility and dividend yield than
the FTSE MIB so that the option will be cheaper to try and aim at an option cost of Eur 5 to
make a 100% protection possible
(D) I will be looking for an underlying asset with lower volatility and a higher dividend
yield than the FTSE MIB so that the option will be cheaper to try and aim at an option cost of

Question 21. A three-year Express investment certificate with coupons that grow over time in case the certificate is not auto-called, is replicated by:
 ☐ (A) Buying the underlying; buying a barrier option call down-and-out; selling a call with strike equal to the express strike; buying a series of digital/barrier puts of knock-out type with strike equal to the express strike, maturities equal to the liquidation dates, in number that increases according to the slope that one wants to impress to the coupon payment schedule ☐ (B) Buying the underlying; buying a barrier option put down-and-out; selling a call with strike equal to the express strike; buying a series of digital/barrier calls of knock-out type with strike equal to the express strike, maturities equal to the liquidation dates, in number that increases according to the slope that one wants to impress to the coupon payment schedule ☐ (C) Buying a zero-coupon bond; buying a barrier option call down-and-in; selling a call with strike equal to the express strike; buying a series of digital/barrier puts of knock-out type with strike equal to the express strike, maturities equal to the liquidation dates, in number that increases according to the slope that one wants to impress to the coupon payment schedule ☐ (D) None of the above
Question 22. During 2014, in Italy the four categories of investment certificates that have raised the most interest in terms of total amounts issued and placed are, in the order: (A) Equity protection; express; bonus; credit linked (B) Equity protection; double win; outperformance; credit linked (C) Bonus; express; equity protection; credit linked (D) None of the above
Question 23. Consider the pricing of multi-underlyings Bonus investment certificates. You are considering three potential features: (i) a Bonus written on a linear basket of stocks, i.e whose payoff depends on the portfolio returns; (ii) a Bonus written on a basket of stocks under the "Worst Of" feature; (iii) a Bonus written on a basket of stocks under the "Best Of feature. All else being equal, which certificate will have the higher bonus amount?
 ☐ (A) The Bonus written on a linear basket of stocks ☐ (B) The Bonus written on a basket of stocks under the "Best Of" feature ☐ (C) The Bonus written on a basket of stocks under the "Worst Of" feature ☐ (D) None of the above

Question 24. Perform the following calculations and answer the related questions.

24a (1 point). Complete the following table concerning the P&L of a fixed, x3 fixed leverage certificate. Is the performance of the certificate the same as "3 times the index performance"? If not, why?

	Underlying	Daily Performance	x3 Leveraged Index	Daily peformance of x3 Leveraged Index
Day 1	100	-7.00%	100	
Day 2		13.00%		
Day 3		-3%		
Day 4		-8%		
Total				

24b (0.5 points). Complete the following table concerning the P&L of a fixed, x3 leveraged certificate. Can you notice any difference vs. 12a? Where are these likely to come from?

	Underlying	Daily Performance	x3 Leveraged Index	Daily peformance of x3 Leveraged Index
Day 1	100	-1.75%	100	
Day 2		3.25%		
Day 3		-0.75%		
Day 4		-2.00%		
Total				

24c (1 point). Complete the following table concerning the P&L of a fixed, x3 leveraged certificate. Can you notice any difference vs. 12a and 12b? Where are these likely to come from?

	Underlying	Daily Performance	x3 Leveraged Index	Daily peformance of x3 Leveraged Index
Day 1	100	-3.87%	100	
Day 2		3.01%		
Day 3		-3.00%		
Day 4	-	-2.37%		
Total	I			

24d (0.5 points) What alternative type of structured product (investment certificate) would allow you to escape the effects of compounding? What would be the costs of such a choice?