

Università Commerciale Luigi Bocconi

M. Guidolin -- Intro Lecture (Remote, Asynchronous)

Professor Massimo Guidolin

20135 – Theory of Finance, Part I (Sept. –October)

Fall 2020

Outline and objectives

- An introduction to quantitative financial economics, with the goal of building a common basis for all the first-year students in view of the specialized courses of the following semesters
- Part I of the course specializes in the theory and practice of optimal portfolio choice
 - Standard knowledge of mathematics and statistics is assumed
- Two goals: build concepts and tools for part II (less exciting) and to give an overview of issues and topics in asset management, possibly with interviews in sight
- Statistics and Quant/Math Prep courses were offered between the end of August and early September 2020 and that the material covered in those 37 hours represent essential background, see
 2020/2021 - 20356 STATISTICS - PREPARATORY COURSE classes 3 and 4 in Blackboard
 2020/2021 - 20550 QUANTITATIVE METHODS FOR FINANCE - PREPARATORY COURSE classes 1 and 2 in Blackboard
 - The goal is to build **concepts** and an overall framework with applications to cases: no memorizing of proofs is expected

Assessment (the exams)

- The exam is written and closed-book
- The weight of this part of the exam is up to 11 points out of 32
- The structure and length of the exam is decided by the course director: I will provide one question with the structure below and he will decide whether to assign it and other details
- Each class (live or recorded asynchronously will close with an essay type question of the type 1°
- Each of the 2021 exams of part 1 of 20135 will include one such question to allow you to prepare and organize a coherent approach

Question 1A (ca. 7.25 points): essay-type

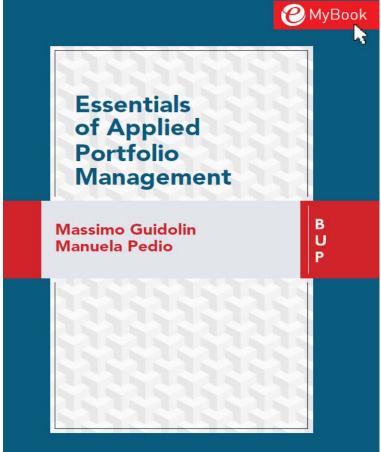
Question 1B (ca. 3 points): case/application

Question 2C (0.75 points): essay-type on one reading (not in slides)

 The material covered in the course is outlined in lecture slides in the My Contents/Sessions entry of the course Blackboard page

The textbook

- The course is exclusively based on selected chapters from:
 - Guidolin, M, and M., Pedio, 2016, Essentials of Applied Portfolio Management, EGEA and Bocconi University Press
- The book contains all that is needed to excel in the exam
- One sample question with the same structure/style as the Respondus-style exam will be made available in Blackboard
- The classes are organized to be self-cointained, unless exceptions are explicitly announced
- Classes, live and recorded give you added value in terms of: (i) to know what topics are important, (ii) to learn in real time



The syllabus

- The syllabus wants to provide elements on six key questions/topics:
 - The workhorse of quant ptf. management: **mean-variance framework**
 - How do you incorporate **customers' preferences** for risk in asset allocation decisions (aka wealth management/1)?
 - How do optimal portfolio decisions depend on labor/entrepreneural income (background risk), aka wealth management/2
 - Using **sentiment** indicators in asset management: big data, deep machine learning, and artificial intelligence
 - Does it pay out to pick the «good guys»? ESG criteria and constraints in asset management
 - Dynamic, sophisticated asset allocation in action—hedge funds
- A number of interesting questions are left out, alas:
 - Tactical vs. strategic asset allocation under predictable investment opportunities (needs advanced econometrics)
 - How to separate skilled from unskilled ptf. managers (needs asset pricing, part 2 of 20135)

What is asset management? An Overview

Asset management involves a wide range of functions and tasks

- This question is relevant both to the objectives of this course as well as to the career choices of a number of people
- Asset management is the scientific study of strategies and methods useful to the buy-side of the financial system
- The buy-side is composed of institutions and professionals that systematically collect and invest the wealth (positive financial imbalances) of households and firms
- What are the heterogeneous functions and processes that take place within the "asset management box"
 - Qualitative portfolio construction and rotation, "stock picking"
 - Traditionally this has to do more with valuation issues than portfolio management strictly defined (see e.g., <u>https://seekingalpha.com/</u> <u>article/4296789-forecasting-future-results-key-successful-stock-investing-part-2?ifp=0</u>)
 - Quantitative portfolio construction, aka asset allocation
 - Marketing & placement of investment vehicles, how to collect wealth
 - Risk management and performance measurement and reporting 6

What is asset management? An Overview

Sell side

On the sell side you pitch your client's products to various interested investors

Here you try to improve the valuation of your product whether it is an asset or whether securities of your company. side

Buy

On the buy side you represent your client to a specific seller in the market whether they may be security market deals or asset deals

Also you look into reducing the valuation for your client and supervise processes like due diligence and valuation

SELL SIDE

Investment
Banking

Corporate

Commercial
Banking

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BUY SIDE

BUY SIDE

This minicourse (most of what I teach really) is buyside oriented

What is asset management? An Overview

Even though quant-based AM techniques are spreading, stock picking remains alive and well

- This course is mostly about formal, quant-based asset allocation models
 - The familiar techniques you may have heard about are tactical vs. strategic asset allocation
 - Often these techniques require the manager to be active and to apply market timing strategies
- In fact, we shall see that in the perspective of formal asset allocation, stock picking turns out to make little sense
 - What types of institutions apply quant methods? Top banks with AM divisions, hedge funds, large-scale mutual fund family suppliers, and insurance companies (also engaged in asset-liability management)



Dynamic asset allocation: what is it?

An asset allocation problem maps an asset menu, a set of **preferences**, and a sequence of subjective discount factors, into a sequence of **optimal** portfolio weights, possibly subject to constraints

Let's examine a first, sample portfolio choice problem written as:

$$\max_{\{\boldsymbol{\omega}_t\}_{t=0}^{T-1}} \sum_{t=0}^{T} \beta^t U(P_t(\boldsymbol{\omega}_0, \boldsymbol{\omega}_1, ..., \boldsymbol{\omega}_t))$$

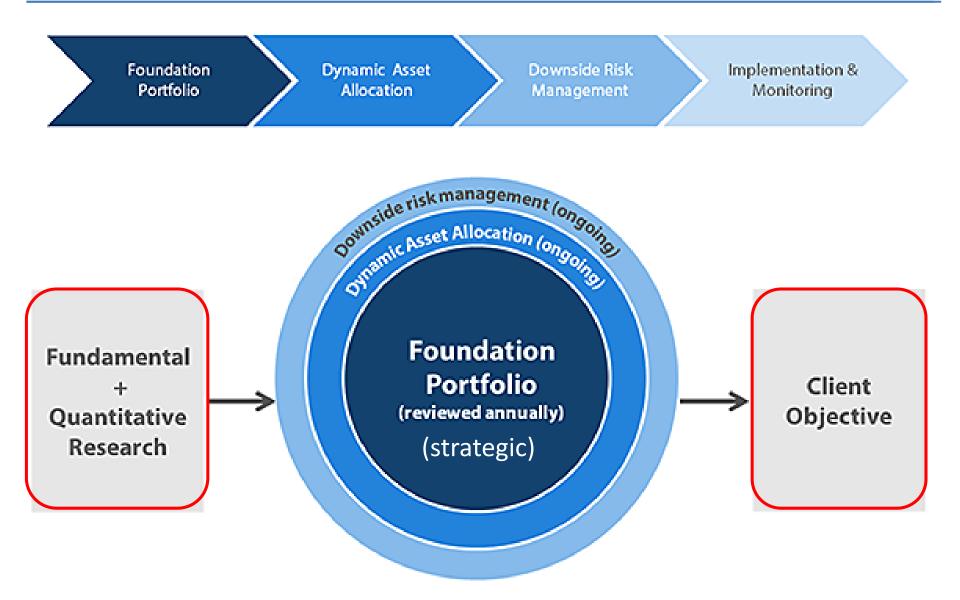
s.t. $\boldsymbol{\omega}_t \in \mathbb{C}$

- o It is a maximization problem
- W.r.t. a N x 1 vector of portfolio weights **ω**, where N is the number of alternative assets (possibly, securities, we may choose from)

✓ N and which securities we can choose from define the asset menu

- We maximize the present discounted sum of the realized values of some function U(•) that measures our level of happiness and therefore reflects preferences
 - We shall often write of a (Von Neumann-Morgenstern) utility function
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Dynamic asset allocation: an overview



Dynamic asset allocation: an overview

An asset allocation problem maps an asset menu, a set of preferences, and a sequence of **subjective discount factors**, into a sequence of optimal portfolio weights, possibly subject to constraints

$$\max_{\{\boldsymbol{\omega}_t\}_{t=0}^{T-1}} \sum_{t=0}^{T} \beta^t U(P_t(\boldsymbol{\omega}_0, \boldsymbol{\omega}_1, ..., \boldsymbol{\omega}_t))$$

s.t. $\boldsymbol{\omega}_t \in \mathbb{C}$

- The sum of "felicity levels" is discounted at a subjective rate β
 - ✓ Time "0" means today, now
 - **✓** Subjective because β does not have to be an interest rate
 - ✓ Because β performs a discounting operation, we normally assume that $\beta \in (0,1]$
- $P_t(\omega_0, \omega_1, ..., \omega_t)$ is a performance criterion, for instance, realized **portfolio return**: N t

$$P_t(\boldsymbol{\omega}_0, \boldsymbol{\omega}_1, \dots, \boldsymbol{\omega}_t) = R_t^p = \sum_{n=1}^{\infty} \sum_{\tau=1}^{\infty} \omega_{n,\tau-1} r_{n,\tau}$$

Dynamic asset allocation: an overview

An asset allocation problem maps an asset menu, a set of preferences, a sequence of subjective discount factors into a sequence of optimal portfolio weights, possibly subject to constraints

$$\max_{\{\boldsymbol{\omega}_t\}_{t=0}^{T-1}} \sum_{t=0}^{T} \beta^t U(P_t(\boldsymbol{\omega}_0, \boldsymbol{\omega}_1, ..., \boldsymbol{\omega}_t))$$

s.t. $\boldsymbol{\omega}_t \in \mathbb{C}$

- The sequence of portfolio weights may be restricted to belong to some set ℂ
 - E.g., short sales may be restricted or impossible outright
 - Almost all institutional investors must fulfill maximum investment rules/criteria (positive diversification constraints)
 - Occasionally, more technical constraints may be imposed: e.g., a portfolio that maximizes utility subject to a value-at-risk constraint
- Even though the entire sequence $\{\omega_0, \omega_1, ..., \omega_t\}$ gets selected, many problems do allow that future weight revisions be taken into account (rebalancing case) 12

Under the assumptions of the EUT, one ranks assets/securities on the basis of the expectation of the utility of their payoffs across states

Under the six axioms detailed in Lecture 4 of the Prep Course, there exists a cardinal, continuous, time-invariant, real-valued Von Neumann-Morgenstern (VNM) felicity function of money U(·), such that for any two lotteries/gambles/securities (i.e., probability distributions of monetary payoffs) x and y,

 $x \gtrsim y$ if and only if $E[U(x)] \ge E[U(y)]$

where for a generic lottery z (e.g., one that pays out either x or y),

 $\mathbb{U}(z) \equiv E[U(z)] = \sum_{s=1}^{s} Prob(state = s)U(z(s))$

- The perceived, cardinal happiness of a complex and risky menu of options, is given by the weighted average of the satisfaction derived from each such individual option, weighted by the probabilities
 - In the following example we use a VNM utility function $U(z) = \ln(z)$
 - The ranking by the EU criterion differs from MV: while according the latter only securities B and D are dominated (by A and C), and hence A and C cannot be ranked, according to EU, security A ranks above security C (and B and D) M. Guidolin -- Intro Lecture 13

State	Security A		Secu	Security B		Security C		Security D	
	Pay-	Prob.	Pay-	Prob.	Pay-	Prob.	Payoff	Prob.	
	off		off		off		-		
i	20	3/15	18	3/15	18	3/15	5	3/15	
ii	18	5/15	18	5/15	16	5/15	14	4/15	
iii	14	4/15	10	4/15	12	4/15	14	4/15	
iv	10	2/15	5	2/15	12	2/15	18	2/15	
V	6	1/15	5	1/15	8	1/15	18	1/15	
$E[R_i]$	15.47		13	13.27		14.27		13.00	
Stdev[R_i]	4.10		5.	5.33		2.91		4.29	
$E[lnR_i]$	2.6	2.693		2.477		2.635		2.483	

Review of Basic Concepts (Prep Course)/1

- In words, under some specific conditions (the axioms), ranking lotteries/gambles/securities on the basis of an investor's preferences or on the basis of the
 - o Expected value
 - Of the happiness that each payoff from the lottery/gamble/security provides,
 - As measured by some cardinal felicity function $U(\cdot)$,

 $\mathbb{U}(z) \equiv E[U(z)] = \sum_{s=1}^{s} Prob(state = s)U(z(s))$

lead to the same choice

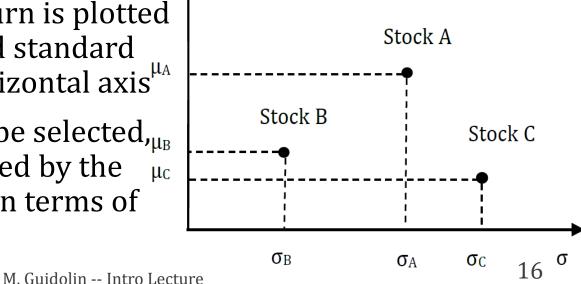
Any **linear affine, monotone increasing transformation** of a VNM utility function ($V(\cdot) = a + bU(\cdot), b > 0$) represents the same preferences

- Arbitrary monotone transformations of cardinal utility functions do not preserve ordering over lotteries
- The VNM representation is preserved under linear affine, increasing transformations: if U(·) is a VNM felicity function, then

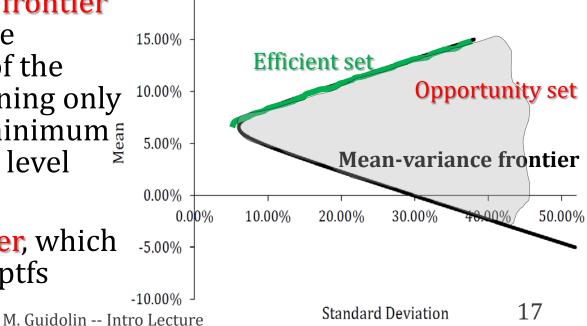
 $V(\cdot) = a + bU(\cdot)$ b > 0 is also a VNM felicity

- This is because $V((x,y;\pi)) = a+bU((x,y;\pi))$ = $a+b[\pi U(x)+(1-\pi)U(y)]$ = $\pi[a+bU(x)]+(1-\pi)[a+bU(y)]=\pi V(x)+(1-\pi)V(y)$
- E.g., if John's felicity function is $U_{John}(R_i) = \ln(R_i)$ and Mary's felicity is instead $U_{Mary}(R_i) = -2 + 4\ln(R_i)$, Mary and John will share the same preferences
- However, when $U_{Mary}(R_i) = +1000 \ln(R_i)$ or $U_{Mary}(R_i) = (\ln(R_i))^3$, this will not be the case

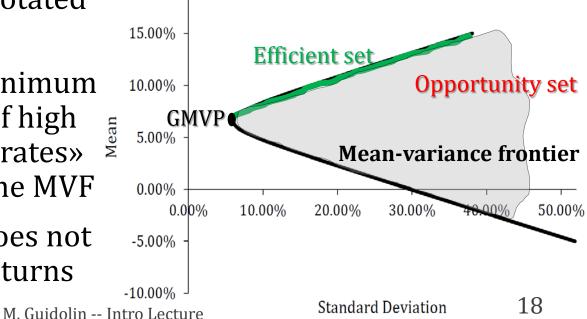
- Prep course reviews the development of the celebrated meanvariance framework introduced by Markowitz in the 1950s
- Initially at least, risky assets only, no borrowing or lending
- Assume that for some reasons, the joint distribution of asset returns is completely characterized by their means, variances, and covariances
- We represent each asset (and portfolio of assets) in a twodimensional diagram, where ^µ expected portfolio return is plotted on the vertical axis and standard deviation is on the horizontal axis^{µA}
- Not all securities may be selected,_{μB}
 e.g., stock C is dominated by the μc remaining two stocks in terms of MV dominance



- According to MV criterion a portfolio is efficient if and only if there is no other portfolio that allows the investor to achieve the same expected return with a lower level of risk or a higher level of expected return with the same level of risk
- Three key notions: i) the opportunity set (feasible region), which includes all the portfolios (both efficient and inefficient) that the investor is able to build given securities in the asset menu
- (ii) the mean-variance frontier (aka minimum variance frontier, MVF) subset of the opportunity set containing only the portfolio(s) with minimum variance for any target level of expected returns
 20.00%
 20.00%
- (iii) the efficient frontier, which only includes efficient ptfs

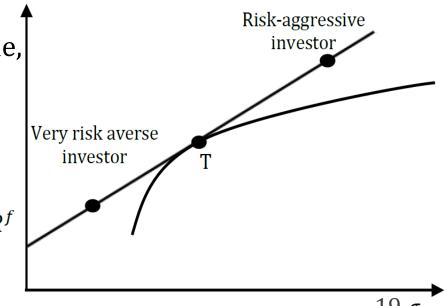


- Because it is possible that a portfolio exists which has a higher return than another portfolio with the same level of risk, only portfolios that have a higher expected return than the global minimum variance portfolio (GMVP) are efficient
- The preferences of the investor(s) for risk are not relevant to the determination of the efficient frontier
- In the classical standard dev.-mean space, the MVF is not a function, but a «right-rotated hyperbola"
 15.00%
 Efficient set
- The GMPV is Global Minimum Variance Ptf. and it is of high interest because «separates» the efficient set from the MVF
- The structure GMVP does not depend on expected returns



Under no frictions and homogeneous beliefs, there exists a tangency ptf. that maximizes the slope of the transformation line

- Assuming beliefs are homogeneous, there are no frictions or taxes, and that individuals face the same R^f and identical asset menus, all rational, non-satiated investors hold the same tangency portfolio
- It is combined with a certain share of risk-free lending or borrowing
- While the share of wealth an investor lends or borrows at R^f depends on the investor's preference for risk, the risky portfolio should be the same for all the investors
- The steepest CTL gets a special name, the Capital Market Line (CML)
- Special case of two-fund separation
- To determine the tangency ptf. one needs to solve: $\max_{\{\omega\}} \frac{(\omega'\mu - R^f)}{(\omega'\Sigma\omega)^{\frac{1}{2}}} \qquad R^f$ subject to $\omega'\iota = 1$



Where to Review Basic Concepts

- Elementary choice under uncertainty: dominance and mean-variance
 - o Guidolin-Pedio, chapter 1, sec. 2
- Preference representation theorem and its meaning
 - o Guidolin-Pedio, chapter 2, sec. 1.1
- Expected utility theorem
 - Guidolin-Pedio, chapter 2, sec. 1.2
- Uniqueness of EU preferences up to monotone increasing linear transformations
 - Guidolin-Pedio, chapter 2, sec. 1.2
- Mean-variance and efficient frontiers: logical meaning
 - Guidolin-Pedio, chapter 3, sec. 1
- The case of no borrowing and lending and two risky assets
 - Guidolin-Pedio, chapter 3, sec. 1.1
- Generalizations to the case of N risky assets and two-fund separation
 - Guidolin-Pedio, chapter 3, sec. 1.2
- Extension to unlimited borrowing and lending
 - Guidolin-Pedio, chapter 3, sec. 2